

This article aims to establish the use of soft-information-based methods for Localization-of-Things and to quantify their performance gain with respect to classical ones.

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ABSTRACT | Location awareness is vital for emerging Internetof-Things applications and opens a new era for Localizationof-Things. This paper first reviews the classical localization techniques based on single-value metrics, such as range and angle estimates, and on fixed measurement models, such as Gaussian distributions with mean equal to the true value of the metric. Then, it presents a new localization approach based on soft information (SI) extracted from intra- and inter-node measurements, as well as from contextual data. In particular, efficient techniques for learning and fusing different kinds of SI are described. Case studies are presented for two scenarios in which sensing measurements are based on: 1) noisy features and non-line-of-sight detector outputs and 2) IEEE 802.15.4a standard. The results show that SI-based localization is highly efficient, can significantly outperform classical techniques, and provides robustness to harsh propagation conditions.

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KEYWORDS | Localization, wireless networks, learning, soft information, Internet-of-Things, Localization-of-Things.

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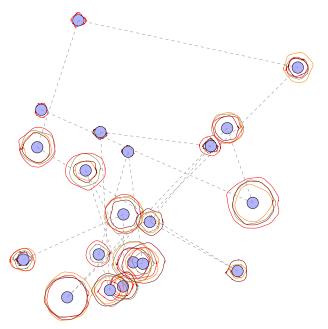


Fig. 1. Pictorial view of LoT relying on SI: blue circles represent nodes, dashed lines represent wireless connectivity between nodes, and red contours represent the SI values associated with node positions.

I. INTRODUCTION

Location awareness enables numerous wireless applications that rely on information associated with the positions of nodes, such as anchors, agents, and targets in wireless networks [1]–[5]. These applications include autonomy [6]–[10], crowd sensing [11]–[19], smart environments [20]–[25], assets tracking [26]–[30], and the Internet-of-Things (IoT) [31]–[36]. The process of locating, tracking, and navigating any possible collaborative or non-collaborative nodes (devices, objects, people,

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and vehicles) is referred to as *Localization-of-Things (LoT)*. The positional information of network nodes is encapsulated by SI, the ensemble of positional and environmental information, respectively, associated with measurements and contextual data. The SI can be extracted via sensing measurements (e.g., using radio, optical, and inertial signals) and contextual data (e.g., using digital map, dynamic model, and node profile). Fig. 1 shows a pictorial view of Localization-of-Things (LoT) relying on SI associated with each node. Accurate LoT depends on reliable acquisition and exploitation of SI, which can be challenging, especially in harsh wireless propagation environments. In particular, conventional approaches based on fixed models are often inadequate for describing SI as a function of the operating environment, signal features, and filtering techniques.

The demand for accurate localization is growing rapidly despite the difficulty in extracting positional information from the received waveforms in most wireless environments. Research in localization and navigation has been carried out along four main strands: 1) fundamental limits [37]-[46]; 2) algorithm design [47]-[79]; 3) network operation [80]-[91]; and 4) network experimentation [92]-[96]. Conventional approaches to localization typically rely on the estimation of single values, such as distances and angles from inter-node measurements, and accelerations and orientations from intra-node measurements. In particular, conventional approaches divide the localization process into two stages: 1) a singlevalue estimation stage in which distances, angles, accelerations, or other position-dependent quantities are estimated and 2) a localization stage in which prior knowledge and single-value estimates (SVEs) serve as inputs to a localization algorithm for position inference. For example, in conventional range-based localization and navigation, the positions of agents or targets are inferred from anchor positions and distance estimates [59]-[61]. Localization accuracy obtained by such methods depends heavily on the quality of the SVEs [96]–[114].

Typically, the accuracy and reliability of conventional localization techniques degrade in wireless environments due to biases in SVEs caused by multipath propagation and non-line-of-sight (NLOS) conditions. Performance limits on ranging were established in [115]-[127], while tractable models for range information were derived in [51]. To cope with wireless propagation impairments, conventional localization approaches focus on improving the estimation of single values [97]-[102], [128], [129]. Techniques to refine the SVE have been exploited by relying on models for SVEs errors (e.g., the bias induced by NLOS conditions) [98], [128], [129]. In addition, received waveforms containing reliable positional information can be selected based on the features extracted from their samples [130]. Data fusion techniques can be used to improve the performance of SVE-based localization by considering the SVE of different features as independent [131]-[133] or by involving hybrid models that account for the relationship among different features [134]-[137].

To overcome the limitations of SVE-based localization, one-stage techniques that employ measurements to directly obtain positions based on a prior model, namely direct positioning (DP), have been explored [138]-[146]. Recently, localization techniques that rely on a set of possible values rather than on single distance estimates (DEs), namely soft range information (SRI), have been developed [55]. In particular, algorithms to learn SRI based on unsupervised machine learning have been developed. To improve the localization performance, it is essential to design localization networks that exploit SI, such as SRI or soft angle information (SAI), together with environmental information, such as contextual data. Contextual data for localization include digital maps, dynamic models, and user profiles [147]-[155].

The LoT scenarios offer the possibility to exploit different sensors that have limited resources for communication, computing, and memory [156]-[164]. In fact, unleashing the multisensor LoT requires fusion of data and measurements collected from heterogeneous sensors with limited resources for communication, computing, and memory [5], and design of efficient network operation strategies [80], [81], [85], [88], [90], [91], [165]–[167]. Multisensor LoT calls for distributed implementation of SI-based localization capable of fusing information from multimodal measurements and environmental knowledge. In addition, distributed localization algorithms require the communication of messages [47]-[49], [168], which may involve high dimensionality depending on the kind of SI. Therefore, it is vital to develop techniques for reducing the dimensionality of SI to make message passing amenable for SI-based localization.

The fundamental questions related to SI for localization and navigation are:

- what gain can be reaped with SI-based methods compared to classical ones;
- how the SI can be learned from sensing measurements such as received waveform samples;
- would SI be enriched by fusing information from different observables and information from the environment; and
- can SI-based algorithms for LoT be implemented efficiently and distributively?

The answers to these questions provide insights into the evolution of positional information at different stages of the localization process, which are essential for the design and analysis of localization systems. The goal of this paper is to establish the use of SI-based methods for LoT and quantify their performance gain with respect to classical ones. We advocate the exploitation of SI, which opens the way to a new level of accuracy for LoT.

This paper establishes SI-based methods for localization and navigation. In particular, it describes the techniques for learning the SI and determines the benefits of fusing different types of positional information. It also demonstrates that SI is much richer than SVEs for localization and navigation. The key contributions of this paper include the following:

- introduction of SI-based techniques for LoT;
- methods for learning and fusing SI that is extracted from sensing measurements and contextual data; and
- quantification of the benefits provided by SI-based techniques compared to SVE-based and DP techniques.

Case studies are presented for two scenarios in which sensing measurements are based on: 1) noisy features and NLOS detection and 2) IEEE 802.15.4a standard.

The remaining sections are organized as follows. Section II provides an overview of techniques for LoT. Section III defines SI for localization in terms of positional and environmental information. Section IV describes how SI can be exploited in localization and navigation. Section V provides the performance benchmarks for SI-based localization. Section VI presents the learning algorithms and data set reduction methods for SI-based localization. Section VII provides the performance results for different case studies. Finally, Section VIII summarizes this paper.

Notations: \mathbb{R} denotes the set of real numbers (\mathbb{R}^+ for non-negatives) and \mathbb{R}^M its *M*th Cartesian power. Random variables (RVs) are displayed in sans-serif, upright fonts; their realizations in serif, italic fonts. Vectors are denoted by bold lowercase letters. For example, an RV and its realization are denoted by \times and x, respectively; a random vector and its realization are denoted by x and x, respectively. The function $f_{x}(x)$ and, for brevity when possible, f(x) denote the probability density function (PDF) of a continuous RV x; $f_{x|y}(x|y)$ and, for brevity when possible, $f(\mathbf{x}|\mathbf{y})$ denote the PDF of x conditional on $\mathbf{y} = \mathbf{y}$; $\varphi(\boldsymbol{x}; \boldsymbol{m}, \boldsymbol{\Sigma})$ denotes the PDF of a Gaussian random vector **x** with mean *m* and covariance matrix Σ ; operators $\mathbb{E}\{\cdot\}$, $\mathbb{V}\{\cdot\}$, and $\mathbb{P}\{\cdot\}$ denote, respectively, the expectation, variance, and probability of the argument, and $\mathbb{E}_{x}\{\cdot\}$ denotes the expectation with respect to RV x. Sets are denoted by calligraphic fonts, e.g., \mathcal{Y} , and empty set is denoted by \emptyset . For a matrix A and a vector a, the transpose is denoted by A^{T} and a^{T} , respectively; tr{A} denotes the trace of the matrix A; and \otimes denotes the Kronecker product of matrices. The norm of a vector u is denoted by ||u||. A positional feature vector, a measurement vector,¹ and contextual data are, respectively, denoted by θ , y, and μ . This paper considers both Bayesian and non-Bayesian formulations; in the former case, the relevant parameters are modeled as random.

II. LOCALIZATION OF THINGS

This section provides the problem setting, discusses the key aspects, and introduces the techniques for LoT.

A. Preliminaries

A localization network is composed of $N_{\rm a}$ agents² with index set $\mathcal{N}_{a} = \{1, 2, \dots, N_{a}\}$ at unknown positions, and $N_{\rm b}$ anchors with index set $\mathcal{N}_{\rm b} = \{N_{\rm a} + 1, N_{\rm a} + 2, \dots, N_{\rm a} + 1\}$ $N_{\rm b}$ at known positions. Both the measurement collection and the localization process are performed at discrete time instants, t_n , with index set $\mathcal{N}_t = \{1, 2, \dots, N_t\}$. The goal is to determine the positional state of agents at different time instants. The positional state of agent i at time t_n , for $i \in$ \mathcal{N}_{a} and $n \in \mathcal{N}_{\mathrm{t}}$, is denoted by $\boldsymbol{x}_{i}^{(n)} \in \mathbb{R}^{D}$ and includes the position $p_i^{(n)}$ and other mobility parameters, such as velocity $v_i^{(n)}$, acceleration $a_i^{(n)}$, orientation $\phi_i^{(n)}$, and angular velocity $\omega_i^{(n)}$. The concatenation of all agents' positional states and the concatenation of all agents' positions are denoted by $x_{\mathcal{N}_{\mathrm{a}}}$ and $p_{\mathcal{N}_{\mathrm{a}}}$, respectively. Localization techniques determine each position estimate \hat{p}_i based on a collection of measurements $\{\boldsymbol{y}_{i,j}\}_{j \in \mathcal{N}}$, where $\mathcal{N} \subseteq \mathcal{N}_{a} \cup \mathcal{N}_{b}$ is the index set of nodes involved in measurements exchange with cardinality N, and on prior information, such as previous positional states and environmental information.

Measurements are related to a feature vector $\boldsymbol{\theta}$ that is a function of node positional states.³ Therefore, the positional information can be extracted from the measurements related to nodes i and j at time t_n , denoted by $oldsymbol{y}_{i,j}^{(n)}$ for $i,j \in \mathcal{N}_{\mathrm{a}} \cup \mathcal{N}_{\mathrm{b}}$ and $n \in \mathcal{N}_{\mathrm{t}},$ where $i \neq j$ and i = j correspond to inter- and intra-node measurements, respectively. An inter-node measurement between nodes i and j is related to positional states x_i and x_j , respectively. Inter-node measurements are commonly obtained by radio measurement units and can include the entire set of received waveform samples or metrics, such as received signal strength (RSS) [169]-[173], time-of-arrival (TOA) [174]-[178], timedifference-of-arrival (TDOA) [179]-[181], angle-of-arrival (AOA) [181]-[184], and Doppler shift [185]-[187]. An intra-node measurement of node i is related to the positional state x_i . Intra-node measurements are commonly obtained by inertial measurement units (IMUs) and can include magnetic field intensity measurements, Doppler shift measurements, force measurements, and angular velocity measurements [151]-[153].

The environmental information μ_i of agent *i* can be used to enforce constraints on positional states. It is commonly composed of digital maps, dynamic models, and agent profiles [147]–[153]. A digital map for agent *i* is related to its position $p_i^{(n)}$ or consecutive positions $p_i^{(n-1)}$ and $p_i^{(n)}$, a dynamic model for agent *i* is related to consecutive positional states $x_i^{(n-1)}$ and $x_i^{(n)}$, and an agent profile for agent *i* is related to its positional state $x_i^{(n)}$. In particular, digital maps can be used to discard positions that do not comply with the map (e.g., outside of a room or building or not on a street) [147]–[149], dynamic models can be used

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¹In general, a measurement vector is a collection of measurements obtained by different types of sensors.

²Agents refer to any possible collaborative or non-collaborative nodes to be localized, including devices, objects, people, and vehicles.

³For brevity, the dependence of θ on node positional states will not explicitly be written in the following.

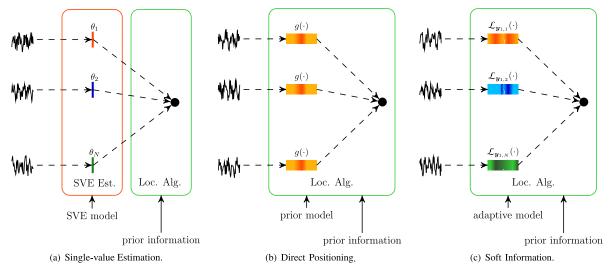


Fig. 2. Sketches of localization techniques based on single values, direct positioning, and soft information.

to express a positional state conditional to a previous state (e.g., moving within a certain speed interval and in a favorable direction) [188]–[191], and agent profiles can be used to enforce the relationships among positional state components (e.g., to enforce zero lateral and vertical velocities for vehicles when measured acceleration and angular velocity fall below given thresholds) [151]–[155].

The performance of localization systems is strongly affected by the quality of sensing measurements. For example, partial or complete blockage of line-of-sight (LOS) propagation conditions leads to positively biased range estimates for time-based ranging [92]. In fact, harsh wireless propagation conditions, such as NLOS, can result in highly biased estimates. Those impairments can be mitigated by detecting the wireless propagation conditions causing the bias. In such scenarios, a measurement vector is $\boldsymbol{y} = [\boldsymbol{z}^{T}, \delta]^{T}$, where \boldsymbol{z} is a measurement vector related to a feature vector $\boldsymbol{\theta}$ and $\delta \in \{0, 1\}$ is the NLOS detector outcome with 0 and 1 corresponding to detecting LOS and NLOS conditions, respectively.⁴ Detection errors are accounted for by means of posterior probabilities of error

$$\epsilon_{\text{NLOS}} \triangleq \mathbb{P}\{\text{NLOS}|\delta = 0\} = \frac{p_{\text{NLOS}}}{P_0} \mathbb{P}\{\delta = 0|\text{NLOS}\}$$
 (1a)

$$\epsilon_{\text{LOS}} \triangleq \mathbb{P}\{\text{LOS}|\delta = 1\} = \frac{1 - p_{\text{NLOS}}}{1 - P_0} \mathbb{P}\{\delta = 1|\text{LOS}\}$$
(1b)

where $p_{\text{NLOS}} = \mathbb{P}\{\text{NLOS}\} = 1 - \mathbb{P}\{\text{LOS}\}$ is the probability of NLOS condition and $P_0 = \mathbb{P}\{\delta = 0\} = 1 - \mathbb{P}\{\delta = 1\}$.

Classical approaches for identifying channel conditions are based on hypothesis testing, for example, on binary hypothesis testing between the LOS and NLOS conditions. Binary hypothesis testing can be extended to multiple hypothesis testing to identify one out of many (more than two) situations, for example, related to the number of obstacles (e.g., walls and furniture) that electromagnetic waves must traverse [92]. A key step in designing the decision rule is choosing the appropriate set of features extracted from the received waveforms. The examples of features include delay spread, maximum amplitude, and kurtosis [98]–[101], [128], [129].⁵

Inference methods can be classified according to how agent positions are inferred (see Fig. 2) as described in the following.

B. SVE-Based Techniques

Classical techniques based on SVEs determine the position of agent $i \in \mathcal{N}_{a}$ in two stages [see Fig. 2(a)] as described in the following.

- (i) Estimation of Single Values: Determine SVEs { θ̂_{i,j}} from inter- or intra-node measurements { y_{i,j}}_{j∈N}.
- (ii) *Positional Inference:* Infer the positions p_i from SVEs { (
 *θ*_{i,j} }_{j∈N} using SVE-based algorithms (e.g., range-based or angle-based algorithms).

The first stage processes each sensing measurement $y_{i,j}$ to obtain an SVE $\hat{\theta}_{i,j}$, such as DE for range-based localization [192]–[205] and angle estimate (AE) for direction-based localization [206]–[209]. The second stage infers the agent position p from the SVEs $\hat{\theta}$, obtained in the first stage, using cooperative or non-cooperative algorithms.

An advantage of classical SVE-based techniques is that the first stage can be accomplished by independent procedures for each measurement $y_{i,j}$. This can result in robust techniques since each measurement can be processed in a different manner (e.g., different procedures for processing measurements in LOS or NLOS conditions). Another advantage of classical SVE-based techniques is that the positional inference stage is simplified as its inputs are single values (e.g., multilateration localization algorithms).

⁴For generic nodes, times, and features, the corresponding subscripts and superscripts will be omitted.

⁵In LOS conditions, the first path in the received signal is typically the strongest. LOS propagation conditions typically give rise to smaller delay spread and larger kurtosis compared with NLOS conditions [130].

A disadvantage of classical SVE-based techniques is that the SVEs do not capture all the positional information contained in sensing measurements, such as received waveform samples.

The localization accuracy of the two-stage approaches can be improved by the following:

- (i) refining SVEs based on environmental information [92]; and
- (ii) discarding SVEs from the measurements that are unreliable for providing agent positional information [130]-[133].

Features extracted from sensing measurements can provide information useful in deciding whether a measurement is representative of the agent position or not (i.e., it contains information about agent position or it is due only to noise and background clutter) [130]. In cases where sensing measurements are not representative, they can be discarded and the corresponding SVEs are not used in the location inference. Other methods based on SVEs detect NLOS propagation conditions and then mitigate the errors on feature estimates when NLOS conditions are detected [97]-[101], [128], [129]. NLOS conditions typically introduce a bias β on the expected value of the feature due to obstructed propagation. Therefore, the SVE $\hat{\theta}$ for a measurement z based on the minimum-meansquare-error (MMSE) criterion is given by [55]

$$\hat{\theta} = \begin{cases} (1 - \epsilon_{\rm NLOS})z + \epsilon_{\rm NLOS}(z - \beta), & \text{for } \delta = 0\\ \epsilon_{\rm LOS}z + (1 - \epsilon_{\rm LOS})(z - \beta), & \text{for } \delta = 1. \end{cases}$$
(2)

Note that when the NLOS detector is highly reliable $(\epsilon_{\rm NLOS} \approx 0, \epsilon_{\rm LOS} \approx 0)$, the bias due to the obstructed propagation is correctly subtracted to refine the SVE [92]. However, in the presence of NLOS detector error, SVEs are biased by $-(1 - \epsilon_{\text{LOS}})\beta$ in LOS cases and by $(1 - \epsilon_{\text{NLOS}})\beta$ in NLOS cases. For additive Gaussian noise with standard deviation σ and $\epsilon_{\text{NLOS}} = \epsilon_{\text{LOS}} = \epsilon$, the mean-square-error (MSE) of the MMSE estimator is found to be

$$\mathbb{E}\left\{\left|\hat{\theta}-\theta\right|^{2}\right\} = \epsilon(1-\epsilon)\beta^{2} + \sigma^{2}.$$
(3)

This reduces to σ^2 , which is the MSE in LOS propagation conditions, when the NLOS detector is totally reliable $(\epsilon = 0).$

C. Direct Positioning Techniques

DP techniques [138]-[146] estimate the position of agent i by relying on the measurement model

$$\mathbf{y}_{i,j} = g(\boldsymbol{\theta}_{i,j}) + \mathbf{n} \tag{4}$$

where the function $g(\cdot)$ is the same for all $j \in \mathcal{N}$ [see Fig. 2(b)], $\theta_{i,j}$ depends on the positions of nodes *i* and j, and n represents additive white Gaussian noise. The position of node $i \in \mathcal{N}_{\mathrm{a}}$ is estimated as the maximum likelihood (ML) or least squares (LS) estimate based on (4). An advantage of DP techniques is that they can improve the localization accuracy with respect to SVEbased techniques since more information, intrinsically contained in sensing measurements, is used. Another advantage is that when using a tractable $q(\cdot)$ together with independent, identically distributed Gaussian noise for each measurement, DP techniques can result in efficient implementations. A disadvantage of DP is that it is nonrobust in scenarios involving different propagation conditions (e.g., some measurements obtained in LOS and some other in NLOS). Another disadvantage is that it provides an inadequate performance when the knowledge of the function $g(\cdot)$ or the distribution of the noise **n** is not sufficiently accurate.

D. SI-Based Techniques

The SI-based techniques [55] directly use sensing measurements $y_{i,j}$ from node $j \in \mathcal{N}$ to infer the position of node *i* by relying on the SI $\mathcal{L}_{y_{i,j}}(\boldsymbol{\theta}_{i,j})$, which varies from measurement to measurement [see Fig. 2(c)]. Such SI can encapsulate all the positional information in each sensing measurement. Then, the agent position p_i can be inferred from SI $\{\mathcal{L}_{\boldsymbol{y}_{i,j}}(\cdot)\}_{j\in\mathcal{N}}$.

An advantage of SI-based localization techniques is that the SI $\mathcal{L}_{u}(\theta)$ can be obtained distributively by N independent procedures tailored to the specific propagation conditions (e.g., either LOS or NLOS). Another advantage is that it can improve the localization accuracy by exploiting all the positional information in each sensing measurement. A disadvantage of SI-based localization techniques is that estimating the SI can be more complicated than estimating SVE.

To better understand the differences in models used for DP and SI-based techniques, Fig. 3 shows the examples of distance likelihood function $\mathcal{L}_{y}(d)$ for a fixed measurement y, as a function of d, under different settings. The parameter $p_{\rm NLOS}$ indicates the probability of NLOS propagation conditions. Fig. 3(a) and Fig. 3(b) show the likelihood functions for a fixed sensing measurement y given by the maximum value of the ultrawide-band (UWB) waveforms in IEEE 802.15.4 a indoor residential and outdoor channels [210], respectively. The figures compare the empirical likelihood function and the Gaussian approximation (a model typically used in DP) using the empirical mean and variance. It can be seen from Fig. 3(a) and Fig. 3(b) that the Gaussian approximation is close to the empirical one in LOS conditions ($p_{\text{NLOS}} = 0$), whereas it becomes less accurate as $p_{\rm NLOS}$ increases. In particular, the maxima of Gaussian approximations and empirical likelihoods occur at different distances in severe NLOS conditions and in equiprobable LOS/NLOS conditions. On the other hand, by attempting to learn the empirical likelihood, SI-based techniques can exploit richer information for

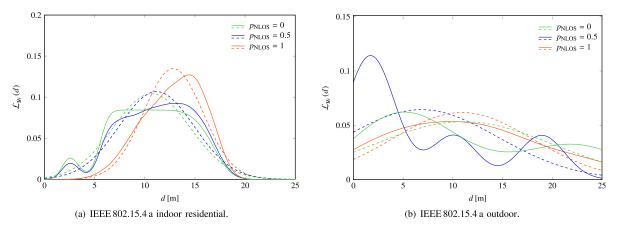


Fig. 3. Examples of distance likelihood functions in two IEEE 802.15.4 a channels with NLOS probability p_{NLOS} = 0 (red line), 0.5 (blue line), and 1 (green line). Empirical likelihoods (continuous lines) and Gaussian likelihoods with empirical mean and variance (dashed lines) are shown.

better localization performance compared to SVE-based and DP techniques, especially in harsh propagation environments.

Remark 1: Note that while DP considers the same form of likelihood function regardless of the propagation conditions for all sensing measurements, SI-based localization utilizes different forms of likelihood functions for measurements in different propagation conditions, as shown in Fig. 2. Observe that SI-based techniques reduce to DP or SVE-based techniques in specific cases. If $\mathbf{y}_{i,j} = \boldsymbol{\theta}_{i,j} + \mathbf{n}$ with \mathbf{n} Gaussian noise, then the three approaches are equivalent. If the likelihood $\mathcal{L}_{\boldsymbol{y}_{i,j}}(\boldsymbol{\theta}_{i,j})$ is proportional to a Gaussian PDF, then the approach based on SI is equivalent to that based on SVE. If the PDF $f(\boldsymbol{\theta}_{i,j}|\boldsymbol{y}_{i,j})$ is proportional to $f_{\mathbf{n}}(\boldsymbol{y}_{i,j} - g(\boldsymbol{\theta}_{i,j}))$, where $f_{\mathbf{n}}(\cdot)$ is the PDF of a zero-mean Gaussian random vector, then the approach based on SI is equivalent to DP.

III. SOFT INFORMATION FOR LOCALIZATION

SI is composed of soft feature information (SFI) and soft context information (SCI): SFI is the ensemble of positional information associated with measurements and SCI is the ensemble of environmental information associated with contextual data. SI-based localization infers agent positions by exploiting both SFI and SCI.

A. Soft Feature Information

SFI for a measurement y is a function of the feature vector θ given by⁶

$$\mathcal{L}_{\boldsymbol{y}}(\boldsymbol{\theta}) \propto f_{\boldsymbol{y}|\boldsymbol{\theta}}(\boldsymbol{y}|\boldsymbol{\theta})$$
 (5a)

$$\mathcal{L}_{\boldsymbol{y}}(\boldsymbol{\theta}) \propto f_{\boldsymbol{y}}(\boldsymbol{y}; \boldsymbol{\theta})$$
 (5b)

where (5a) and (5b) display the Bayesian and non-Bayesian formulation, respectively; in the latter case, SFI coincides with the likelihood function of feature vector θ . Different types of measurements give rise to different SFI. For instance, the SFI associated with range-related, anglerelated, and velocity-related measurements is, respectively, given by $\mathcal{L}_{y}(d)$, $\mathcal{L}_{y}(\alpha)$, and $\mathcal{L}_{y}(v)$.

Refer to the example scenario in Fig. 4(a) with two anchors (red annulus) and an agent (blue circle). The anchor in the bottom-left collects the range-related measurements, from which the SRI of Fig. 4(b) is obtained. The anchor in the top-right collects angle-related measurements, from which the SAI of Fig. 4(c) is obtained. Thus, the SFI provides richer information than its SVE $\hat{\theta}$ by quantifying the odds of different θ values. The use of SFI enables soft-decision localization instead of classical hard-decision localization.

B. Soft Context Information

SCI is a function of the feature vector θ provided by contextual data μ . Different types of contextual data, such as digital maps, dynamic models, and agent profiles, give rise to different kinds of SCI as described next. The SCI provided by a map can be incorporated as a prior distribution of the position [147] (e.g., certain positions in the map are very unlikely) or as a conditional distribution of the position at time step *n*, given the position at time step n - 1 (e.g., mobility in a corridor is more likely along the corridor then in a perpendicular direction). In the former case, the SCI is proportional to a prior distribution that depends on μ as

$$\Phi_{\boldsymbol{\mu}}(\boldsymbol{p}) \propto f_{\boldsymbol{\mathsf{P}}}(\boldsymbol{p};\boldsymbol{\mu}) \tag{6}$$

while, in the latter case, it is proportional to a conditional PDF that depends on μ as

$$\Phi_{\mu}(\boldsymbol{p}^{(n)}, \boldsymbol{p}^{(n-1)}) \propto f_{\mathbf{p}^{(n)}|\mathbf{p}^{(n-1)}}(\boldsymbol{p}^{(n)}|\boldsymbol{p}^{(n-1)}; \boldsymbol{\mu}).$$
(7)

⁶The SFI and SCI are defined up to a proportionality constant, which is sufficient for SI-based localization.

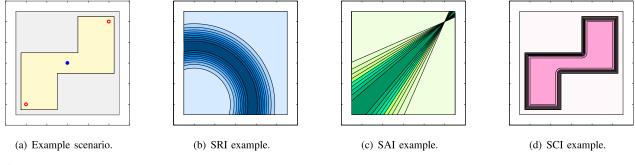


Fig. 4. Examples of scenario and associated SI. The area is 120 m \times 120 m; for the associated SI, darker colors refer to larger values.

SCI provided by a dynamic model can be incorporated as a conditional distribution of the positional state at time step *n*, given the positional state at time step n - 1 (e.g., consecutive positions close to each other are highly likely for an agent with low speed; similar considerations apply to consecutive velocities for cars in a highway) [150]. Therefore, SCI associated with a dynamic model μ is proportional to a conditional PDF depending on μ

$$\Phi_{\mu}(\boldsymbol{x}^{(n)}, \boldsymbol{x}^{(n-1)}) \propto f_{\mathbf{x}^{(n)}|\mathbf{x}^{(n-1)}}(\boldsymbol{x}^{(n)}|\boldsymbol{x}^{(n-1)}; \boldsymbol{\mu}).$$
(8)

A widely used dynamic model is that based on a linearization of the positional state evolution via Taylor expansion and on Gaussian noise, leading to

$$\Phi_{\boldsymbol{\mu}}(\boldsymbol{x}^{(n)}, \boldsymbol{x}^{(n-1)}) \propto \varphi(\boldsymbol{x}^{(n)}; \boldsymbol{F}\boldsymbol{x}^{(n-1)}, \boldsymbol{\Sigma}_d)$$
(9)

where F is known as the transition matrix and Σ_d is the covariance of the process noise, both depending on μ .

SCI provided by an agent profile can be incorporated as a distribution of several components in the positional state. For instance, if the agent is a pedestrian carrying the IMU on a foot, low values of acceleration and angular velocity correspond to high likelihood for the low values of velocity [153]. Therefore, the SCI provided by such agent profile μ is proportional to a joint PDF of acceleration **a**, angular velocity ω , and velocity **v** as

$$\Phi_{\boldsymbol{\mu}}(\boldsymbol{a},\boldsymbol{\omega},\boldsymbol{v}) \propto f_{\boldsymbol{a},\boldsymbol{\omega},\boldsymbol{v}}(\boldsymbol{a},\boldsymbol{\omega},\boldsymbol{v};\boldsymbol{\mu}). \tag{10}$$

For example, if the agent is a car, the misalignments of velocity vector and the direction of the car are highly unlikely. Therefore, SCI provided by such agent profile μ is proportional to a PDF of the angle γ between velocity **v** and heading **h** as

$$\Phi_{\mu}(\gamma) \propto f_{\gamma}(\gamma; \mu). \tag{11}$$

Refer to the example scenario in Fig. 4(a) with SCI given by the environment map shown in Fig. 4(d). The SCI provides additional information on positional states, thus

improving the performance of both soft-decision localization and classical hard-decision localization.

C. Data Fusion Based on Soft Information

The exploitation of SI for localization also enables the efficient fusion of sensing measurements and contextual data via multiplication of the corresponding SFI and SCI.

Sensing measurements gathered with different modalities can be fused efficiently by multiplying their corresponding SFI as long as the different measurement vectors are conditionally independent, given the positional features. Such conditional independence is generally satisfied as long as the measurement vectors are obtained from different sensors. In particular, for measurement set $\mathcal{Y} =$ $\{\boldsymbol{y}^{(k)}\}_{k=1}^{K_{\rm F}}$ related to the feature set $\Theta = \{\boldsymbol{\theta}^{(k)}\}_{k=1}^{K_{\rm F}}$, with each measurement $\boldsymbol{y}^{(k)}$ related to feature $\boldsymbol{\theta}^{(k)}$ for k = $1, 2, \ldots, K_{\rm F}$, SFI can be written as

$$\mathcal{L}_{\mathcal{Y}}(\Theta) = \prod_{k=1}^{K_{\mathrm{F}}} \mathcal{L}_{\boldsymbol{y}^{(k)}}(\boldsymbol{\theta}^{(k)}).$$
(12)

D. Soft Information in Harsh Propagation Environments

SI can encapsulate all the positional information inherent in the sensing measurements obtained in harsh propagation environments even with errors on the detection of propagation conditions. Consider a measurement vector $\boldsymbol{y} = [\boldsymbol{z}^{\mathrm{T}}, \delta]^{\mathrm{T}}$, where \boldsymbol{z} is a measurement vector related to a feature vector $\boldsymbol{\theta}$ and δ is the NLOS detector outcome, as described in Section II-A. Assuming a constant reference prior for $\boldsymbol{\theta}$ [211], the SFI of \boldsymbol{y} is given by [55]

$$\mathcal{L}_{\boldsymbol{y}}(\boldsymbol{\theta}) \\ \propto \begin{cases} (1 - \epsilon_{\rm NLOS}) \mathcal{L}_{\boldsymbol{z}_{\rm LOS}}(\boldsymbol{\theta}) + \epsilon_{\rm NLOS} \mathcal{L}_{\boldsymbol{z}_{\rm NLOS}}(\boldsymbol{\theta}) & \text{for } \boldsymbol{\delta} = 0 \\ \epsilon_{\rm LOS} \mathcal{L}_{\boldsymbol{z}_{\rm LOS}}(\boldsymbol{\theta}) + (1 - \epsilon_{\rm LOS}) \mathcal{L}_{\boldsymbol{z}_{\rm NLOS}}(\boldsymbol{\theta}) & \text{for } \boldsymbol{\delta} = 1 \end{cases}$$
(13)

where $\mathcal{L}_{z_{\text{LOS}}}(\cdot)$ and $\mathcal{L}_{z_{\text{NLOS}}}(\cdot)$ denote the SFI for measurements collected in LOS and NLOS conditions, respectively.

For instance, consider a 1-D measurement model

$$z = \theta + n \tag{14}$$

where n represents the Gaussian noise with PDF

$$f_{n}(n) = \begin{cases} \varphi(n; 0, \sigma_{\text{LOS}}^{2}), & \text{for LOS cases} \\ \varphi(n; \beta, \sigma_{\text{NLOS}}^{2}), & \text{for NLOS cases} \end{cases}$$
(15)

in which β denotes the bias due to NLOS propagation. In such a case

$$\mathcal{L}_{z_{\text{LOS}}}(\theta) = \varphi(\theta; z, \sigma_{\text{LOS}}^2)$$
(16a)

$$\mathcal{L}_{z_{\text{NLOS}}}(\theta) = \varphi(\theta; z - \beta, \sigma_{\text{NLOS}}^2).$$
 (16b)

When the detector is highly reliable ($\epsilon_{\rm NLOS} \approx 0, \epsilon_{\rm LOS} \approx 0$), SFI is concentrated around the true feature, i.e., $\mathcal{L}_{z_{\rm LOS}}(\theta)$ for LOS and $\mathcal{L}_{z_{\rm NLOS}}(\theta)$ for NLOS propagation conditions. Moreover, SI-based techniques are more robust to detect errors than classical techniques, as the SFI in (13) accounts for the error probability of the detector and considers both the true and biased features.

IV. SI-BASED LOCALIZATION

An SI-based localization system operates according to the following steps:

- (i) acquisition of feature-related measurements and contextual data;
- (ii) characterization of the SFI and SCI provided by each measurement and contextual data; and
- (iii) position inference by exploiting SFI and SCI.

To illustrate the benefits of SI for localization, we now describe how SFI and SCI can be utilized to infer the positions of the agents $\{p_i\}_{i \in N_a}$ from measurements y and contextual data μ .⁷ Recall that the feature vector θ inherent in y is related to the node positions p. We describe the following:

- localization without cooperation, where sensing measurements and contextual data are related only to one agent at a single time instant;
- network localization with spatial cooperation among agents, where sensing measurements and contextual data are related to neighboring agents at a single time instant;
- navigation with temporal cooperation, where sensing measurements and contextual data are related only to one agent at consecutive time instants; and
- network navigation with spatiotemporal cooperation, where sensing measurements and contextual data are

⁷For notational convenience, consider that for each pair of nodes *i* and *j*, there is a measurement vector $\boldsymbol{y}_{i,j}$ or a contextual data vector $\boldsymbol{\mu}_i$ available. The expressions with unavailable measurements or data for some node pairs can be obtained by removing the terms corresponding to those pairs.

related to neighboring agents at consecutive time instants.

A. SI-Based Localization without Cooperation

In non-cooperative localization systems, the positions of the agents are inferred based on measurements with respect to the anchors and contextual data. By modeling the positions of agents as unknown parameters, the maximum likelihood (ML) estimate of the position of agent $i \in \mathcal{N}_{\rm a}$ is [55]

$$\hat{\boldsymbol{p}}_{i} = \arg \max_{\boldsymbol{p}_{i}} f(\{\boldsymbol{y}_{i,j}\}_{j \in \mathcal{N}_{\mathrm{b}}} | \boldsymbol{p}_{i})$$
$$= \arg \max_{\boldsymbol{p}_{i}} \prod_{j \in \mathcal{N}_{\mathrm{b}}} \mathcal{L}_{\boldsymbol{y}_{i,j}}(\boldsymbol{\theta}_{i,j}).$$
(17)

If all the SFI in (17) are Gaussian with mean $\theta_{i,j}$, then the ML estimator leads to the LS estimator and to the weighted least squares (WLS) estimator, respectively, for cases with the same variance and different variances for $j \in \mathcal{N}_{\rm b}$.

By modeling the positions of agents as RVs, contextual data can be incorporated directly. The position of agent $i \in N_a$ can be inferred from the posterior distribution. In particular, the MMSE and the maximum *a posteriori* (MAP) estimates are given by the mean and mode of the posterior distribution, respectively, as [55]

$$\hat{\boldsymbol{p}}_{i} = \int \boldsymbol{p}_{i} f(\boldsymbol{p}_{i} | \{ \boldsymbol{y}_{i,j} \}_{j \in \mathcal{N}_{\mathrm{b}}}; \boldsymbol{\mu}_{i}) d\boldsymbol{p}_{i}$$
(18a)

$$\hat{\boldsymbol{p}}_{i} = \arg \max_{\boldsymbol{p}_{i}} f(\boldsymbol{p}_{i} | \{\boldsymbol{y}_{i,j}\}_{j \in \mathcal{N}_{\mathrm{b}}}; \boldsymbol{\mu}_{i})$$
(18b)

where for the posterior distribution

$$f(\boldsymbol{p}_{i}|\{\boldsymbol{y}_{i,j}\}_{j\in\mathcal{N}_{\mathrm{b}}};\boldsymbol{\mu}_{i}) \propto \Phi_{\boldsymbol{\mu}_{i}}(\boldsymbol{p}_{i}) \prod_{j\in\mathcal{N}_{\mathrm{b}}} \mathcal{L}_{\boldsymbol{y}_{i,j}}(\boldsymbol{\theta}_{i,j}).$$
(19)

The contextual data μ_i may depend on the previously estimated position of node *i* (e.g., a map-aided 3-D localization in which the map for node *i* depends on whether the previously estimated position for node *i* was on a certain floor). Note that the MAP estimator in (18b) coincides with the ML estimator when contextual data are not available (i.e., $\Phi_{\mu_i}(\mathbf{p}_i)$ constant with respect to \mathbf{p}_i).

B. SI-Based Localization with Spatial Cooperation

In network localization systems [1], the positions of the agents are inferred based on the measurements with respect to neighboring agents, in addition to those with respect to the anchors, and to contextual data. By modeling the positions of agents as unknown parameters, the ML estimate of the positions of all the agents is [55]

$$\hat{\boldsymbol{p}}_{\mathcal{N}_{\mathrm{a}}} = \operatorname*{arg\,max}_{\boldsymbol{p}_{\mathcal{N}_{\mathrm{a}}}} f\Big(\{\boldsymbol{y}_{i,j}\}_{\substack{i \in \mathcal{N}_{\mathrm{a}} \\ j \in \mathcal{N}_{\mathrm{a}} \cup \mathcal{N}_{\mathrm{b}}}} \Big| \boldsymbol{p}_{\mathcal{N}_{\mathrm{a}}}\Big)$$
$$= \operatorname*{arg\,max}_{\boldsymbol{p}_{\mathcal{N}_{\mathrm{a}}}} \prod_{\substack{i \in \mathcal{N}_{\mathrm{a}} \\ j \in \mathcal{N}_{\mathrm{a}} \cup \mathcal{N}_{\mathrm{b}}}} \mathcal{L}_{\boldsymbol{y}_{i,j}}(\boldsymbol{\theta}_{i,j}).$$
(20)

If all the SFI used in (20) is Gaussian with mean $\theta_{i,j}$, then the ML estimate leads to LS or WLS estimates as in the non-cooperative case.

By modeling the positions of agents as random variables (RVs), contextual data can be incorporated directly. The MMSE and the MAP estimates of all agent positions can be obtained analogously to (18) using the posterior distribution

$$f\left(\boldsymbol{p}_{\mathcal{N}_{\mathrm{a}}}|\{\boldsymbol{y}_{i,j}\}_{\substack{i\in\mathcal{N}_{\mathrm{a}}\\j\in\mathcal{N}_{\mathrm{a}}\cup\mathcal{N}_{\mathrm{b}}}}^{i\in\mathcal{N}_{\mathrm{a}}};\boldsymbol{\mu}_{\mathcal{N}_{\mathrm{a}}}\right)$$

$$\propto\prod_{i\in\mathcal{N}_{\mathrm{a}}}\left[\Phi_{\boldsymbol{\mu}_{i}}(\boldsymbol{p}_{i})\prod_{j\in\mathcal{N}_{\mathrm{a}}\cup\mathcal{N}_{\mathrm{b}}}\mathcal{L}_{\boldsymbol{y}_{i,j}}(\boldsymbol{\theta}_{i,j})\right].$$
(21)

Note that the MAP estimate coincides with ML estimate when contextual data are not available.

C. SI-Based Navigation with Temporal Cooperation

Navigation systems [1] infer the positions of the agents at different time instants based on inter-node measurements from the anchors, intra-node measurements, and contextual data. When positional states and measurements can be described by an hidden Markov model (HMM) over time steps from 1 to n + 1, the posterior distribution of positional state for each agent can be obtained sequentially [53]. In particular, $f(\boldsymbol{x}_i^{(n+1)}|\mathcal{Y}_i^{(1:n+1)};\boldsymbol{\mu}_i)$ can be obtained by performing a prediction step using a dynamic model

$$f(\boldsymbol{x}_{i}^{(n+1)}|\mathcal{Y}_{i}^{(1:n)};\boldsymbol{\mu}_{i}) \\ \propto \int \Phi_{\boldsymbol{\mu}_{i}}(\boldsymbol{x}_{i}^{(n+1)},\boldsymbol{x}_{i}^{(n)})f(\boldsymbol{x}_{i}^{(n)}|\mathcal{Y}_{i}^{(1:n)};\boldsymbol{\mu}_{i}) d\boldsymbol{x}_{i}^{(n)}$$
(22)

followed by an update step using a new measurement:

$$f\left(\boldsymbol{x}_{i}^{(n+1)} | \mathcal{Y}_{i}^{(1:n+1)}; \boldsymbol{\mu}_{i}\right) \\ \propto \prod_{j \in \mathcal{N}_{\mathrm{b}} \cup \{i\}} \mathcal{L}_{\boldsymbol{y}_{i,j}^{(n+1)}}\left(\boldsymbol{\theta}_{i,j}^{(n+1)}\right) f\left(\boldsymbol{x}_{i}^{(n+1)} | \mathcal{Y}_{i}^{(1:n)}; \boldsymbol{\mu}_{i}\right)$$
(23)

where $\mathcal{Y}_{i}^{(1:k)} = \{ \boldsymbol{y}_{i,j}^{(1:k)} \}_{j \in \mathcal{N}_{\mathrm{b}} \cup \{i\}}$.⁸

If both the SFI and the SCI are Gaussian and linear with respect to positional states, then the updates in (23) can be performed in a closed form such as those in Kalman filters (KFs) [212]–[216]. Otherwise, the implementation of (23) has to resort to approximations accounting for the complexity versus accuracy tradeoff. Examples of such approximations are those used in extended Kalman filters (EKFs) [217], unscented Kalman filters (UKFs) [218], and belief condensation filters (BCFs) [53].

⁸Notation
$$\boldsymbol{y}_{i,i}^{(1:k)}$$
 denotes the set $\{\boldsymbol{y}_{i,i}^{(h)}\}_{h=1}^{k}$.

D. SI-Based Navigation with Spatiotemporal Cooperation

Network navigation systems [1] infer the positions of the agents at different time instants based on internode measurements with respect to both anchors and neighboring agents, intra-node measurements, and contextual data. When positional states and measurements can be described by an HMM over time steps from 1 to n + 1, the joint posterior distribution of positional states can be obtained sequentially [40]. In particular, $f(\boldsymbol{x}_{\mathcal{N}_{a}}^{(n+1)}|\mathcal{Y}^{(1:n+1)};\boldsymbol{\mu}_{\mathcal{N}_{a}})$ can be obtained by performing a prediction step using a dynamic model

$$f\left(\boldsymbol{x}_{\mathcal{N}_{a}}^{(n+1)} \middle| \mathcal{Y}^{(1:n)}; \boldsymbol{\mu}_{\mathcal{N}_{a}}\right) \\ \propto \int \Phi_{\boldsymbol{\mu}_{\mathcal{N}_{a}}}\left(\boldsymbol{x}_{\mathcal{N}_{a}}^{(n+1)}, \boldsymbol{x}_{\mathcal{N}_{a}}^{(n)}\right) f\left(\boldsymbol{x}_{\mathcal{N}_{a}}^{(n)} \middle| \mathcal{Y}^{(1:n)}; \boldsymbol{\mu}_{\mathcal{N}_{a}}\right) d\boldsymbol{x}_{\mathcal{N}_{a}}^{(n)} \quad (24)$$

followed by an update step using a new measurement:

$$f(\boldsymbol{x}_{\mathcal{N}_{\mathrm{a}}}^{(n+1)} | \mathcal{Y}^{(1:n+1)}; \boldsymbol{\mu}_{\mathcal{N}_{\mathrm{a}}}) \\ \propto \prod_{\substack{i \in \mathcal{N}_{\mathrm{a}} \\ j \in \mathcal{N}_{\mathrm{a}} \cup \mathcal{N}_{\mathrm{b}}}} \mathcal{L}_{\boldsymbol{y}_{i,j}^{(n+1)}} (\boldsymbol{\theta}_{i,j}^{(n+1)}) f(\boldsymbol{x}_{\mathcal{N}_{\mathrm{a}}}^{(n+1)} | \mathcal{Y}^{(1:n)}; \boldsymbol{\mu}_{\mathcal{N}_{\mathrm{a}}})$$
(25)

where $\mathcal{Y}^{(1:k)} = \{ \boldsymbol{y}_{i,j}^{(1:k)} \}_{i \in \mathcal{N}_{\mathrm{a}}, j \in \mathcal{N}_{\mathrm{a}} \cup \mathcal{N}_{\mathrm{b}}}.$

If the movement of each agent is independent of any other agent's movement, then

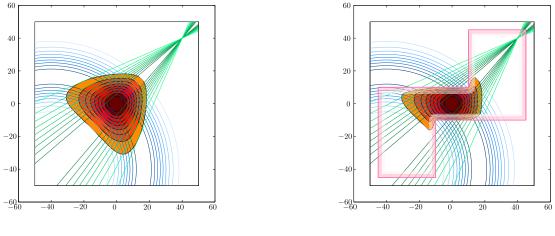
$$\Phi_{\boldsymbol{\mu}_{\mathcal{N}_{\mathrm{a}}}}\left(\boldsymbol{x}_{\mathcal{N}_{\mathrm{a}}}^{(n+1)}, \boldsymbol{x}_{\mathcal{N}_{\mathrm{a}}}^{(n)}\right) = \prod_{i \in \mathcal{N}_{\mathrm{a}}} \Phi_{\boldsymbol{\mu}_{i}}\left(\boldsymbol{x}_{i}^{(n+1)}, \boldsymbol{x}_{i}^{(n)}\right).$$
(26)

If both the SFI and the SCI are Gaussian and linear with respect to positional states, then the updates in (25) can be performed in closed form such as those in KFs [212]–[216]. Otherwise, the implementation of (25) has to resort to approximations accounting for the complexity versus accuracy tradeoff. Examples of such approximations are those used in EKFs [217], UKFs [218], and BCFs [53].

E. SI-Based vs. SVE-Based Localization

SI-based localization is a new approach that exploits richer information than classical SVE-based localization. Consider, for instance, range and angle inter-node measurements; the SI-based localization relies on SRI and SAI, whereas SVE-based localization relies on DE and AE. Refer to the examples of SFI and SCI in Fig. 4. Fusion of all available SFI and SCI provides enhanced SI (red contoured areas in Fig. 5). In particular, Fig. 5(a) shows the fusion of the SFI corresponding to the SRI in Fig. 4(b) and to the SAI in Fig. 4(c). Fig. 5(b) shows the enhanced SI obtained by fusion of the SRI in Fig. 4(b), the SAI in Fig. 4(c), and the SCI in Fig. 4(d).

Fig. 6 shows an example of comparison between the classical and the new approach. In particular, refer to the



(a) Fusion of SRI and SAI.

(b) Fusion of SRI, SAI, and SCI.

Fig. 5. Example of data fusion for enhanced SI (red contoured area): the coordinates on the axes are in meters.

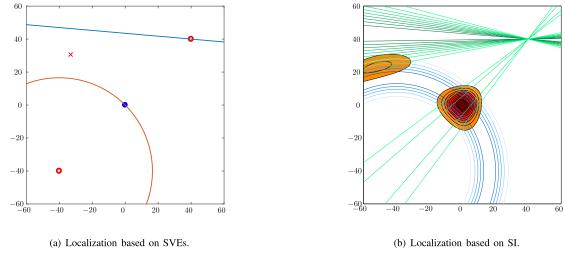


Fig. 6. Example of SVEs versus SI-based localization: the coordinates on the axes are in meters.

scenario shown in Fig. 4(a) where the bottom-left anchor provides range measurements to the target, whereas the top-right anchor provides angle measurements. Due to the harsh propagation environment, the angle measurements are affected by a bias, which results in an erroneous AE for SVE-based localization, while it results in bimodal SAI for SI-based localization. These two situations are, respectively, shown in Fig. 6(a) and (b). In particular, the cross in Fig. 6(a) represents the wrongly estimated position using the LS algorithm with DE and AE as the inputs, whereas the dark red area in Fig. 6(b) shows that the maximum of the positional feature likelihood is near the true position. This simple example illustrates how SI on θ provides richer information than that offered by its SVE $\hat{\theta}$, thus improving the localization accuracy.

F. Distributed Implementation

Distributed implementation is particularly important in scenarios with networks of nodes having limited capabilities such as those in LoT. Cooperation in space and time can improve the localization accuracy. However, the use of measurements related to several agents causes information coupling [219], [220], resulting in highly interrelated inference for different agents. This fact is reflected in the concatenated arguments in the posterior distribution in (21) and (25), compared to that in (19) and (23). The optimal implementation of noncooperative approaches described in (19) and (23) can be performed in a distributed fashion since each agent can determine its own posterior distribution. On the other hand, the optimal implementation of cooperative approaches described in (21) and (25) requires a centralized implementation to determine the joint posterior distribution of all the agents.

Techniques have been developed for distributed implementation by approximating the joint posterior distribution via marginalization. For example, the loopy belief propagation technique approximates the marginal posterior distribution of each agent by disregarding the cycles in the graph describing the network connectivity [49]. Specifically, an approximate marginal

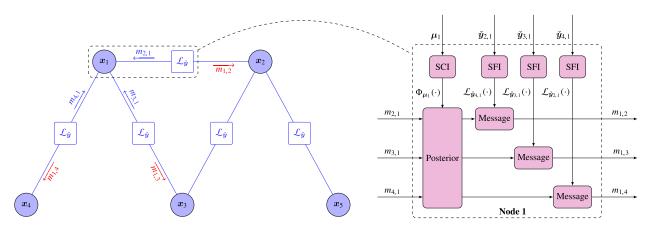


Fig. 7. Example of distributed implementation: (left) network factor graph with message passing involving node 1; and (right) computation based on different SFI and SCI inside node 1.

posterior $\tilde{f}(\boldsymbol{x}_i|\tilde{\mathcal{Y}})$ for the positional state of agent *i* based on the measurement set $\check{\mathcal{Y}} = \{\mathcal{Y}, \check{\boldsymbol{y}}_{i,j}\}$ can be obtained sequentially from $\tilde{f}(\boldsymbol{x}_i|\mathcal{Y})$ when a new measurement $\check{\boldsymbol{y}}_{i,j}$ is available, which is given as

$$\tilde{f}(\boldsymbol{x}_i|\check{\mathcal{Y}}) \propto \tilde{f}(\boldsymbol{x}_i|\mathcal{Y}) m_{j,i}$$
 (27)

where

$$m_{j,i} \propto \int \tilde{f}(\boldsymbol{x}_j | \mathcal{Y}) \mathcal{L}_{\check{\boldsymbol{y}}_{i,j}}(\boldsymbol{\theta}_{i,j}) d\boldsymbol{x}_j$$
 (28)

is usually referred to as message from node j to node i. Equation (27) forms the basis for developing network messaging algorithms.

Fig. 7 shows an example of a network factor graph with messaging for distributed implementation of network localization and navigation (NLN). In particular, messages entering to and exiting from node 1 are highlighted, and the computation blocks inside node 1 are depicted.

V. SOFT INFORMATION AND PERFORMANCE LIMITS

Fundamental limits provide performance benchmarks that are essential for network design. In [37]–[41], a performance measure called squared position error bound has been derived as a function of the Fisher information matrix (FIM). In the following, we will derive the FIM as a function of SFI and SCI.

Let $\mathbf{x}_{\mathcal{N}_{a}}^{\mathcal{N}_{t}}$ be a random vector composed of positional states, for N_{a} agents at N_{t} time instants, in which the $[i + (n - 1)N_{a}]$ th element is $\mathbf{x}_{i}^{(n)}$. The positional state is inferred from inter-node measurements $\mathbf{y}_{i,j}^{(n)}$ related to $\mathbf{x}_{i}^{(n)} - \mathbf{x}_{j}^{(n)}$, intra-node measurements $\mathbf{y}_{i,i}^{(n)}$ related to $\mathbf{x}_{i}^{(n)}$, and a dynamic model $\boldsymbol{\mu}$ related to $\mathbf{x}_{i}^{(n)}$, where $i \in \mathcal{N}_{a}$, $j \in \mathcal{N}_{a} \cup \mathcal{N}_{b}$ with $j \neq i$, and $n, m \in \mathcal{N}_{t}$.

According to the Fisher information inequality, an estimator $\hat{\mathbf{x}}_{i}^{(n)}$ of positional state $\mathbf{x}_{i}^{(n)}$ satisfies

$$\mathbb{E}\left\{\left\|\hat{\mathbf{x}}_{i}^{(n)}-\mathbf{x}_{i}^{(n)}\right\|^{2}\right\} \geq \operatorname{tr}\left\{\left[\boldsymbol{J}^{-1}\right]_{i}^{(n)}\right\}$$
(29)

where $[J^{-1}]_i^{(n)}$ denotes the $[i + (n - 1)N_a]$ th $D \times D$ diagonal block in the inverse of the Bayesian FIM [221] for positional states $\mathbf{x}_{\mathcal{N}_a}^{\mathcal{N}_t}$. The FIM for $\mathbf{x}_{\mathcal{N}_a}^{\mathcal{N}_t}$ is given by [40]

$$\boldsymbol{J} = \boldsymbol{J}_{\rm p} + \boldsymbol{J}_{\rm s} + \boldsymbol{J}_{\rm t} \tag{30}$$

where $J_{\rm p}$ is the FIM corresponding to prior knowledge of $\mathbf{x}_{N_{\rm a}}^{N_{\rm t}}$; $J_{\rm s}$ is the FIM consisting of two terms: the first term corresponds to the inter-node measurements (with anchors) and the second corresponds to the spatial cooperation (with other agents); and $J_{\rm t}$ is the FIM consisting of two terms: the first term corresponds to the intra-node measurements (at a particular time step) and the second corresponds to temporal cooperation (between different time steps). In particular

$$\boldsymbol{J}_{\mathrm{s}} = \underbrace{\sum_{i \in \mathcal{N}_{\mathrm{a}}} \boldsymbol{G}_{i,i}^{(n,n)} \otimes \sum_{j \in \mathcal{N}_{\mathrm{b}}} \boldsymbol{K}_{i,j}^{(n,n)}}_{n \in \mathcal{N}_{\mathrm{t}}} + \underbrace{\sum_{j \in \mathcal{N}_{\mathrm{a}}} \boldsymbol{G}_{i,j}^{(n,n)} \otimes \boldsymbol{K}_{i,j}^{(n,n)}}_{n \in \mathcal{N}_{\mathrm{t}}} + \underbrace{\sum_{i \in \mathcal{N}_{\mathrm{a}}} \boldsymbol{G}_{i,j}^{(n,n)} \otimes \boldsymbol{K}_{i,j}^{(n,n)}}_{n \in \mathcal{N}_{\mathrm{t}}}$$
(31a)

 $J_{t} = \underbrace{\sum_{i \in \mathcal{N}_{a}} G_{i,i}^{(n,n)} \otimes K_{i,i}^{(n,n)}}_{n \in \mathcal{N}_{t}} + \underbrace{\sum_{i \in \mathcal{N}_{a}} G_{i,i}^{(n,m)} \otimes K_{i,i}^{(n,m)}}_{i \in \mathcal{N}_{t} \otimes \mathcal{N}_{t}} + \underbrace{\sum_{i \in \mathcal{N}_{a}} G_{i,i}^{(n,m)} \otimes K_{i,i}^{(n,m)}}_{i \in \mathcal{N}_{a}}$ (31b)

where

$$G_{i,j}^{(n,m)} = \begin{cases} (e_k - e_l)(e_k - e_l)^{\mathrm{T}}, & \text{for } (i,n) \neq (j,m) \\ e_k(e_k)^{\mathrm{T}}, & \text{for } (i,n) = (j,m) \end{cases}$$
(32)

in which $k = [i + (n-1)N_a]$, $l = [j + (m-1)N_a]$, and e_k is an N_aN_t -dimensional vector with all zeros except a one at the *k*th element. The matrices K in (31) will be described in the following.

Define

$$egin{aligned} & \jmath_{ ext{sf}}(oldsymbol{y};oldsymbol{ heta}_1,oldsymbol{ heta}_2,oldsymbol{ heta}_3) riangleq & rac{\partial \ln \mathcal{L}_{oldsymbol{y}}(oldsymbol{ heta})}{\partial oldsymbol{ heta}_1} & rac{\partial \ln \mathcal{L}_{oldsymbol{ heta}}(oldsymbol{ heta})}{\partial oldsymbol{ heta}}$$

for soft features and soft context, respectively, where the parameter vector θ is a function of θ_1 , θ_2 , and the nuisance parameter vector θ_3 . It is important to note that $j_{sf}(y; \theta_1, \theta_2, \theta_3)$ is a function of $\mathcal{L}_y(\theta)$ that depends on the type of measurement y. Similarly, $j_{sc}(\mu; \theta_1, \theta_2, \theta_3)$ is a function of $\Phi_\mu(\theta)$ that depends on the type of contextual data μ . The matrix $K_{i,j}^{(n,m)} \in \mathbb{R}^{D \times D}$ accounts for the pairwise positional information related to agent $i \in \mathcal{N}_a$ at time step $n \in \mathcal{N}_t$ and node $j \in \mathcal{N}_a \cup \mathcal{N}_b$ at time step $m \in \mathcal{N}_t$ as elaborated next.

K^(n,n)_{i,i} accounts for the information that agent *i* obtains at time step *n* from intra-node measurements *y*⁽ⁿ⁾_{i,i}. It can be written as

$$\boldsymbol{K}_{i,i}^{(n,n)} = \mathbb{E}\big\{\jmath_{\mathrm{sf}}(\mathbf{y}_{i,i}^{(n)}; \mathbf{x}_i^{(n)}, \mathbf{x}_i^{(n)}, \emptyset)\big\}.$$
 (33)

2) $K_{i,j}^{(n,n)}$ for $j \in \mathcal{N}_{b}$ accounts for the information that agent *i* obtains at time step *n* from inter-node measurements $y_{i,j}^{(n)}$ with respect to anchor *j*. It can be written as

$$\boldsymbol{K}_{i,j}^{(n,n)} = \mathbb{E}\left\{ j_{\text{sf}}\left(\boldsymbol{y}_{i,j}^{(n)}; \boldsymbol{x}_{i}^{(n)}, \boldsymbol{x}_{i}^{(n)}, \boldsymbol{\emptyset}\right) \right\}.$$
(34)

K^(n,n)_{i,j} for j ∈ N_a \ {i} accounts for the information that agent i obtains at time step n from inter-node measurements *y*⁽ⁿ⁾_{i,j} with respect to neighboring agent j (i.e., spatial cooperation). It can be written as

$$\boldsymbol{K}_{i,j}^{(n,n)} = \mathbb{E}\left\{-\jmath_{\mathrm{sf}}\left(\boldsymbol{\mathsf{y}}_{i,j}^{(n)}; \boldsymbol{\mathsf{x}}_{i}^{(n)}, \boldsymbol{\mathsf{x}}_{j}^{(n)}, \boldsymbol{\emptyset}\right)\right\}.$$
(35)

K^(n,m)_{i,i} accounts for the information that agent *i* obtains at time step *n* from its positional state at previous time step *m* and the dynamic model μ (i.e., temporal cooperation).⁹ It can be written as

$$\boldsymbol{K}_{i,i}^{(n,m)} = \mathbb{E}\left\{-\jmath_{\mathrm{sc}}\left(\boldsymbol{\mu}; \boldsymbol{\mathsf{x}}_{i}^{(n)}, \boldsymbol{\mathsf{x}}_{i}^{(m)}, \boldsymbol{\emptyset}\right)\right\}.$$
(36)

Consider a network with $N_{\rm a} = 3$ agents and $N_{\rm t} = 2$ time steps. The FIM can be written as in (30), in which $J_{\rm s}$ (corresponding to spatial measurements) and $J_{\rm t}$ (cor-

⁹Commonly, dynamic models provide information related to two consecutive time steps, and in those cases, $K_{i,i}^{(n,m)} = \mathbf{0}$ for m < n-1.

responding to temporal measurements) are given by (37) and (38), respectively, at the top of the next two pages. In (37), the first term represents the information coming from inter-node measurements with anchors, while the second term represents the information coming from spatial cooperation with other agents. In (38), the first term represents the information inherent in intra-node measurements at a particular time step, while the second term represents the information coming from temporal cooperation between different time steps.

A. FIM from SI Functions

The building blocks $K_{i,j}^{(n,n)}$ of the FIM for some special cases of SFI are detailed here.

Proposition 1: Consider 2-D node velocity $\mathbf{v}_i^{(n)}$ and node position $\mathbf{p}_i^{(n)}$ and define the direction matrix (DM)

$$\boldsymbol{J}_{\rm dm}(\phi) \triangleq \begin{bmatrix} \cos^2(\phi) & \cos(\phi)\sin(\phi) \\ \cos(\phi)\sin(\phi) & \sin^2(\phi) \end{bmatrix}.$$
 (39)

The blocks $K_{i,j}^{(n,n)}$ related to speed $\|\mathbf{v}_i^{(n)}\|$, range $\mathsf{d}_{i,j}^{(n)}$, and angle $\alpha_{i,j}^{(n)}$ inherent in measurements involving nodes *i* and *j* at time instant *n* are provided in the following.

1) For intra-node measurements related to the speed

$$\boldsymbol{K}_{i,i}^{(n,n)} = \boldsymbol{e}_{i_{v}} \boldsymbol{e}_{i_{v}}^{\mathrm{T}} \otimes \mathbb{E}_{\boldsymbol{v}_{i}^{(n)}} \{\lambda_{\mathrm{s}} \boldsymbol{\mathsf{J}}_{\mathrm{s}}\}$$
(40)

where i_v is the velocity component index in the state vector $\mathbf{x}_i^{(n)}$. In (40), λ_s is the speed information intensity (SII) [220] and \mathbf{J}_s is the DM for speed measurements given by

$$\lambda_{\mathrm{s}} = \mathbb{E}_{\mathbf{y}_{i,i}^{(n)} \mid \mathbf{v}_{i}^{(n)}} \left\{ \jmath_{\mathrm{sf}} \left(\mathbf{y}_{i,i}^{(n)}; \left\| \mathbf{v}_{i}^{(n)} \right\|, \left\| \mathbf{v}_{i}^{(n)} \right\|, \emptyset \right) \right\}$$
(41a)

$$\mathbf{J}_{\rm s} = \boldsymbol{J}_{\rm dm}(\boldsymbol{\alpha}_{\rm v}) \tag{41b}$$

where α_v is the angle between vector $\mathbf{v}_i^{(n)}$ and the horizontal axis.

2) For inter-node measurements related to ranges

$$\boldsymbol{K}_{i,j}^{(n,n)} = \boldsymbol{e}_{i_{\mathrm{p}}} \boldsymbol{e}_{i_{\mathrm{p}}}^{\mathrm{T}} \otimes \mathbb{E}_{\boldsymbol{p}_{i}^{(n)},\boldsymbol{p}_{j}^{(n)}} \{\lambda_{\mathrm{r}} \boldsymbol{\mathsf{J}}_{\mathrm{r}}\}$$
(42)

where $i_{\rm p}$ is the position component index in the state vector $\mathbf{x}_i^{(n)}$. In (42), $\lambda_{\rm r}$ is the range information intensity (RII) [38] and $\mathbf{J}_{\rm r}$ is the DM for range measurements given by

$$\lambda_{\rm r} = \mathbb{E}_{\mathbf{y}_{i,j}^{(n)} | \mathbf{p}_i^{(n)}, \mathbf{p}_j^{(n)}} \left\{ \jmath_{\rm sf} \left(\mathbf{y}_{i,j}^{(n)}; \mathbf{d}_{i,j}^{(n)}, \mathbf{d}_{i,j}^{(n)}, \emptyset \right) \right\}$$
(43a)

$$\mathbf{J}_{\mathrm{r}} = \boldsymbol{J}_{\mathrm{dm}} \left(\boldsymbol{\alpha}_{i,j}^{(n)} \right) \tag{43b}$$

where $\mathbf{d}_{i,j}^{(n)}$ is the Euclidean distance between the *i*th and *j*th nodes, and $\alpha_{i,j}^{(n)}$ is the angle between vector $\mathbf{p}_{j}^{(n)} - \mathbf{p}_{i}^{(n)}$ and the horizontal axis.

$$J_{s} = \begin{bmatrix} \sum_{j \in \mathcal{N}_{b}} K_{1,j}^{(1,1)} & 0 & 0 & 0 & 0 & 0 \\ 0 & \sum_{j \in \mathcal{N}_{b}} K_{2,j}^{(1,1)} & 0 & 0 & 0 & 0 \\ 0 & 0 & \sum_{j \in \mathcal{N}_{b}} K_{3,j}^{(1,1)} & 0 & 0 & 0 & 0 \\ 0 & 0 & \sum_{j \in \mathcal{N}_{b}} K_{1,j}^{(2,2)} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \sum_{j \in \mathcal{N}_{b}} K_{2,j}^{(2,2)} & 0 \\ 0 & 0 & 0 & 0 & 0 & \sum_{j \in \mathcal{N}_{b}} K_{2,j}^{(2,2)} & 0 \\ 0 & 0 & 0 & 0 & 0 & \sum_{j \in \mathcal{N}_{b}} K_{2,j}^{(2,2)} & 0 \\ 0 & 0 & 0 & 0 & 0 & \sum_{j \in \mathcal{N}_{b}} K_{2,j}^{(2,2)} & 0 \\ 0 & 0 & 0 & 0 & 0 & \sum_{j \in \mathcal{N}_{b}} K_{3,j}^{(2,2)} \\ -K_{1,2}^{(1,1)} & -K_{1,2}^{(1,1)} & -K_{1,3}^{(1,1)} & 0 & 0 & 0 \\ -K_{1,2}^{(1,1)} & \sum_{j \in \mathcal{N}_{b} \setminus \{2\}} K_{2,j}^{(1,1)} & -K_{2,3}^{(1,1)} & 0 & 0 & 0 \\ -K_{1,3}^{(1,1)} & -K_{2,3}^{(1,1)} & \sum_{j \in \mathcal{N}_{b} \setminus \{3\}} K_{3,j}^{(1,1)} & 0 & 0 & 0 \\ \hline & 0 & 0 & 0 & \sum_{j \in \mathcal{N}_{b} \setminus \{1\}} K_{1,j}^{(2,2)} & -K_{1,2}^{(2,2)} & -K_{1,3}^{(2,2)} \\ 0 & 0 & 0 & 0 & -K_{1,2}^{(2,2)} & \sum_{j \in \mathcal{N}_{b} \setminus \{2\}} K_{3,j}^{(2,2)} \\ 0 & 0 & 0 & 0 & -K_{1,3}^{(2,2)} & -K_{2,3}^{(2,2)} & \sum_{j \in \mathcal{N}_{b} \setminus \{3\}} K_{3,j}^{(2,2)} \\ \end{bmatrix}$$

3) Finally, for inter-node measurements related to angles From (33)

$$\boldsymbol{K}_{i,j}^{(n,n)} = \boldsymbol{e}_{i_{\mathrm{p}}} \boldsymbol{e}_{i_{\mathrm{p}}}^{\mathrm{T}} \otimes \mathbb{E}_{\boldsymbol{p}_{i}^{(n)}, \boldsymbol{p}_{j}^{(n)}} \{ \boldsymbol{\lambda}_{\mathrm{a}} \boldsymbol{\mathsf{J}}_{\mathrm{a}} \}$$
(44)

where $i_{\rm p}$ is the position component index in the state vector $\mathbf{x}_i^{(n)}$. In (44), $\lambda_{\rm a}$ is the angle information intensity (AII) [41] and $J_{\rm a}$ is the DM for angle measurements given by

$$\lambda_{\mathbf{a}} = \frac{1}{(\mathsf{d}_{i,j}^{(n)})^2} \mathbb{E}_{\mathbf{y}_{i,j}^{(n)} | \mathbf{p}_i^{(n)}, \mathbf{p}_j^{(n)}} \left\{ \jmath_{\mathrm{sf}} \left(\mathbf{y}_{i,j}^{(n)}; \alpha_{i,j}^{(n)}, \alpha_{i,j}^{(n)}, \emptyset \right) \right\}$$
(45a)

$$\mathbf{J}_{\mathrm{a}} = \boldsymbol{J}_{\mathrm{dm}} \left(\boldsymbol{\alpha}_{i,j}^{(n)} + \frac{\pi}{2} \right). \tag{45b}$$

Proof: In what follows, we provide the proof for the case of intra-node measurements $y_{i,i}^{(n)}$ related to speed $\|v_i^{(n)}\|$; the other two cases can be obtained analogously.

$$\boldsymbol{K}_{i,i}^{(n,n)} = \mathbb{E}_{\mathbf{y}_{i,i}^{(n)}, \mathbf{v}_{i}^{(n)}} \left\{ \jmath_{\mathrm{sf}} \left(\mathbf{y}_{i,i}^{(n)}; \mathbf{x}_{i}^{(n)}, \mathbf{x}_{i}^{(n)}, \boldsymbol{\emptyset} \right) \right\}$$

which results in

$$\boldsymbol{K}_{i,i}^{(n,n)} = \boldsymbol{e}_{i_{\mathbf{v}}} \boldsymbol{e}_{i_{\mathbf{v}}}^{\mathrm{T}} \otimes \mathbb{E}_{\boldsymbol{y}_{i,i}^{(n)}, \boldsymbol{v}_{i}^{(n)}} \left\{ \jmath_{\mathrm{sf}} \left(\boldsymbol{y}_{i,i}^{(n)}; \boldsymbol{v}_{i}^{(n)}, \boldsymbol{v}_{i}^{(n)}, \boldsymbol{\emptyset} \right) \right\}$$
(46)

because $y_{i,i}^{(n)}$ are measurements related to velocity. By using the chain rule for derivatives

$$\jmath_{\rm sf}\left(\boldsymbol{y}_{i,i}^{(n)}; \boldsymbol{v}_{i}^{(n)}, \boldsymbol{v}_{i}^{(n)}, \boldsymbol{\emptyset}\right) = \jmath_{\rm sf}\left(\boldsymbol{y}_{i,i}^{(n)}; \left\|\boldsymbol{v}_{i}^{(n)}\right\|, \left\|\boldsymbol{v}_{i}^{(n)}\right\|, \boldsymbol{\emptyset}\right) \\ \times \frac{\partial \left\|\boldsymbol{v}_{i}^{(n)}\right\|}{\partial \boldsymbol{v}_{i}^{(n)}} \left(\frac{\partial \left\|\boldsymbol{v}_{i}^{(n)}\right\|}{\partial \boldsymbol{v}_{i}^{(n)}}\right)^{\rm T} \quad (47)$$

since $\boldsymbol{y}_{i,i}^{(n)}$ are measurements related to speed.

$$J_{t} = \begin{bmatrix} K_{1,1}^{(1,1)} & 0 & 0 & 0 & 0 & 0 \\ 0 & K_{2,2}^{(1,1)} & 0 & 0 & 0 & 0 \\ 0 & 0 & K_{3,3}^{(1,1)} & 0 & 0 & 0 \\ 0 & 0 & 0 & K_{1,1}^{(2,2)} & 0 & 0 \\ 0 & 0 & 0 & 0 & K_{2,2}^{(2,2)} & 0 \\ 0 & 0 & 0 & 0 & 0 & K_{3,3}^{(2,2)} \end{bmatrix} \\ + \begin{bmatrix} K_{1,1}^{(2,1)} & 0 & 0 & -K_{1,1}^{(2,1)} & 0 & 0 \\ 0 & K_{2,2}^{(2,1)} & 0 & 0 & -K_{2,2}^{(2,1)} & 0 \\ 0 & 0 & K_{3,3}^{(2,1)} & 0 & 0 & -K_{3,3}^{(2,1)} \\ -K_{1,1}^{(2,1)} & 0 & 0 & K_{1,1}^{(2,1)} & 0 & 0 \\ 0 & -K_{2,2}^{(2,1)} & 0 & 0 & K_{2,2}^{(2,1)} & 0 \\ 0 & 0 & -K_{3,3}^{(2,1)} & 0 & 0 & K_{3,3}^{(2,1)} \end{bmatrix}$$
(38)

Performing the expectations in (46) using the law of iterated expectations as $\mathbb{E}_{\mathbf{y}_{i,i}^{(n)},\mathbf{v}_{i}^{(n)}}\{\cdot\} = \mathbb{E}_{\mathbf{v}_{i}^{(n)}}\{\mathbb{E}_{\mathbf{y}_{i,i}^{(n)}|\mathbf{v}_{i}^{(n)}}\{\cdot\}\}$, we obtain (40) in which λ_{s} in (41a) and \mathbf{J}_{s} in (41b) result, respectively, from the expectation of the first and second terms in the right-hand side of (47).

Remark 2: Proposition 1 indicates that the measurements related to the speed provide information with intensity λ_s in the direction of $\mathbf{v}_i^{(n)}$, since \mathbf{J}_s has only one eigenvector associated with non-zero eigenvalue in such direction. Similarly, the measurements related to the range provide information with intensity λ_r in the direction of $\mathbf{p}_j^{(n)} - \mathbf{p}_i^{(n)}$, since \mathbf{J}_r has only one eigenvector associated with non-zero eigenvalue in such direction. Finally, the measurements related to the angle provide information with intensity λ_a in the direction orthogonal to $\mathbf{p}_j^{(n)} - \mathbf{p}_i^{(n)}$, since \mathbf{J}_a has only one eigenvector associated with non-zero eigenvalue in such direction.

B. FIM in Harsh Propagation Environments

This section provides the SFI from inter-node measurements when a detector for NLOS propagation conditions is employed, as described in Sections II-A and III-D.

Proposition 2: Consider the inter-node measurement $y_{i,j}^{(n,n)} = [z^{\mathrm{T}}, \delta]^{\mathrm{T}}$, where z is a measurement related to a feature θ and δ is the NLOS detector outcome, as described in Section II-A. When $\mathcal{L}_{y}(\theta)$ follows (13) and z follows the measurement model in (14) and (15) with $\sigma_{\mathrm{LOS}} =$

 $\sigma_{\text{NLOS}} = \sigma$ and $\epsilon_{\text{LOS}} = \epsilon_{\text{NLOS}} = \epsilon$, then the FIM block corresponding to $\mathbf{y}_{i,j}^{(n,n)}$ is given by:

$$\boldsymbol{K}_{i,j}^{(n,n)} = \boldsymbol{e}_{i_{\mathrm{p}}} \boldsymbol{e}_{i_{\mathrm{p}}}^{\mathrm{T}} \otimes \mathbb{E}_{\boldsymbol{\theta}} \{ \lambda_{\boldsymbol{\theta}} \boldsymbol{\mathsf{J}}_{\boldsymbol{\theta}} \}$$
(48)

where λ_{θ} and \mathbf{J}_{θ} have instantiations

$$\lambda_{\theta} = \frac{1}{\sigma^4} [\mathbb{E}_{\mathsf{z}|\theta} \{ (\mathsf{z} - \theta - \chi_0)^2 | \delta = 0 \} \mathbb{P} \{ \delta = 0 \}$$

+ $\mathbb{E}_{\mathsf{z}|\theta} \{ (\mathsf{z} - \theta - \chi_1)^2 | \delta = 1 \} \mathbb{P} \{ \delta = 1 \}]$ (49a)

$$\boldsymbol{J}_{\theta} = \left(\frac{\partial \theta}{\partial \boldsymbol{p}_{i}^{(n)}}\right) \left(\frac{\partial \theta}{\partial \boldsymbol{p}_{i}^{(n)}}\right)^{\mathrm{I}}$$
(49b)

as well as χ_0 and χ_1 have instantiations

$$\chi_0 = \frac{\beta \epsilon \varphi(\theta; z - \beta, \sigma^2)}{(1 - \epsilon) \varphi(\theta; z, \sigma^2) + \epsilon \varphi(\theta; z - \beta, \sigma^2)}$$
(50a)

$$\chi_1 = \frac{\beta \left(1 - \epsilon\right) \varphi(\theta; z - \beta, \sigma^2)}{\epsilon \,\varphi(\theta; z, \sigma^2) + \left(1 - \epsilon\right) \varphi(\theta; z - \beta, \sigma^2)}.$$
 (50b)

Proof: Equation (48) is obtained from Proposition 1 and the fact that

$$\frac{\partial \ln \mathcal{L}_{\boldsymbol{y}_{i,j}^{(n)}}(\theta)}{\partial \theta} = \begin{cases} \frac{1}{\sigma^2} (z - \theta - \chi_0) & \text{for } \delta = 0\\ \frac{1}{\sigma^2} (z - \theta - \chi_1) & \text{for } \delta = 1. \end{cases}$$

Remark 3: For $\epsilon = 0$ and $\mathbb{P}{\{\delta = 0\}} = 1$ (LOS scenarios with totally reliable NLOS detector), the term $\chi_0 = 0$ and (48) results in the known expression for LOS scenarios (i.e., $\lambda = 1/\sigma^2$) [38]. Moreover, the two Gaussian PDFs $\varphi(\cdot)$ in (50a) and (50b) have negligible overlap for $\beta \gg \sigma$, as well as $\chi_0 \approx \chi_1 \approx 0$ (resp. $\chi_0 \approx \chi_1 \approx \beta$) when z has mean θ (resp. $\theta + \beta$) and standard deviation σ . Therefore, for $\beta \gg \sigma$ (48) approximates the $K_{i,j}^{(n,n)}$ for LOS scenarios with totally reliable NLOS detector (i.e., $\lambda \approx 1/\sigma^2$), independent of the detector reliability ϵ .

VI. LEARNING SOFT INFORMATION

Using a Bayesian formulation, the SFI can be determined based on a joint distribution function, referred to as generative model, of the positional feature together with measurements and contextual data. For instance, the SFI inherent in a measurement vector \boldsymbol{y} related to feature $\boldsymbol{\theta}$ can be determined as $\mathcal{L}_{\boldsymbol{y}}(\boldsymbol{\theta}) \propto f_{\mathbf{y},\boldsymbol{\theta}}(\boldsymbol{y},\boldsymbol{\theta})$ in the absence of prior information on $\boldsymbol{\theta}$ or as $\mathcal{L}_{\boldsymbol{y}}(\boldsymbol{\theta}) = f_{\mathbf{y},\boldsymbol{\theta}}(\boldsymbol{y},\boldsymbol{\theta})/f_{\boldsymbol{\theta}}(\boldsymbol{\theta})$ in the presence of prior information on $\boldsymbol{\theta}$ [55]. Analogously, SCI inherent in contextual data $\boldsymbol{\mu}$ related to acceleration \boldsymbol{a} , angular velocity $\boldsymbol{\omega}$, and velocity \boldsymbol{v} can be obtained as $\Phi_{\boldsymbol{\mu}}(\boldsymbol{a},\boldsymbol{\omega},\boldsymbol{v}) \propto f(\boldsymbol{a},\boldsymbol{\omega},\boldsymbol{v};\boldsymbol{\mu})$ [153].

In simple scenarios, the generative model can be accurately determined based on the relation between measurements, positional features, and contextual data. In more complex scenarios, finding an accurate generative model is challenging and it is preferable to learn it using measurements, positional features, and contextual data by a process commonly known as density estimation [222]–[224]. In particular, the SI can be determined by a two-phase algorithm as follows:

- off-line phase where the approximation of the generative model is determined from measurements, positional features, and context data;
- on-line phase where the SFI and SCI for each new measurement are determined based on the generative model learned in the previous phase.

The off-line phase determines the generative models for environments similar to (but not necessarily the same as) those where the localization network will operate (i.e., where the on-line phase is performed). The exploitation of SFI and SCI has a complexity that depends on the generative model learned during the off-line phase; therefore, constraints on the computation and communication capabilities of nodes call for tractable and parsimonious generative models. Techniques, such as belief condensation [53], which approximate complicated distributions by combination of simple ones, can enable the use of tractable generative models for efficient implementation of SI-based localization.

A. SI from Reduced Data Set

Determining the generative model from training data can be difficult, especially for measurement vectors with

Algorithm 1 SFI Estimation with Dimensionality Reduction

Off-line Phase

- 1: Acquire training data $\{y^{(k)}, \theta^{(k)}\}_{k \in \mathcal{N}_{\text{train}}}$ through a measurement campaign realized in time steps indexed by $\mathcal{N}_{\text{train}}$.
- 2: Perform dimensionality reduction of training data:

$$\{\boldsymbol{y}^{(k)}, \boldsymbol{\theta}^{(k)}\}_{k \in \mathcal{N}_{\mathrm{train}}} \to \{\psi(\boldsymbol{y}^{(k)}), \boldsymbol{\theta}^{(k)}\}_{k \in \mathcal{N}_{\mathrm{train}}}.$$

- 3: Determine an approximate generative model $\tilde{f}(\psi(\boldsymbol{y}), \boldsymbol{\theta})$.
- 4: Store the approximate generative model.

On-line Phase

- 1: for $k \ge 0$ do
- 2: Acquire a new measurement vector $y^{(k)}$ at time t_k .
- 3: Perform dimensionality reduction of the new measurement vector:

$$\boldsymbol{y}^{(k)} \to \psi(\boldsymbol{y}^{(k)}).$$

4: Determine the SFI of the reduced measurement vector $\psi(y^{(k)})$ using the stored generative model as

$$\mathcal{L}_{\psi(\boldsymbol{y}^{(k)})}(\boldsymbol{\theta}) = \hat{f}(\psi(\boldsymbol{y}^{(k)}), \boldsymbol{\theta}).$$

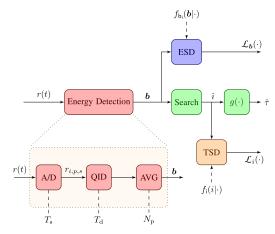
5: end for

high dimensionality (e.g., waveform samples with fine time-delay resolution) [55]. Therefore, dimensionality reduction is crucial for efficient learning of SFI. Such a dimensionality reduction step can be described as a function $\psi(\cdot)$ that transforms a measurement vector $\boldsymbol{y} \in \mathbb{R}^M$ into $\psi(\boldsymbol{y}) \in \mathbb{R}^{M'}$ with M' significantly smaller than M. The dimensionality reduction may not necessarily involve SVEs, while SVEs can be thought of as a specific type of dimensionality reduction. While the proposed SI-based approach can be used for any type of measurement, the dimensionality reduction and generative model learning techniques are technology-dependent.

An algorithm for estimating the SFI with dimensionality reduction is composed of two phases (see Algorithm 1): an off-line phase in which dimensionality reduction $\psi(\cdot)$ is performed¹⁰ and generative models are determined based on training measurements and an on-line phase in which the SFI is learned from the generative model and each measurement collected during operation.

Various techniques can be used for performing dimensionality reduction and determining the generative model. Unsupervised machine learning techniques provide ways to learn SFI. In particular, SRI learning is addressed in [55], where techniques for dimensionality reduction based on physical features, principal component analysis (PCA), and Laplacian eigen-map are introduced and techniques for determining generative models based on Fisher-Wald setting and kernel density estimation are presented.

 ${}^{10}\text{Clearly}, \ \psi(\boldsymbol{y}^{(k)}) = \boldsymbol{y}^{(k)}$ in the absence of dimensionality reduction.



(a) Energy detection-based range information: use of b for obtaining the DE and the SRI based on energy-based soft-decision (ESD) and threshold-based soft-decision (TSD).

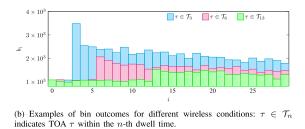


Fig. 8. Range information from energy detection.

Energy detection-based techniques are often used to determine information on the TOA τ of the received signal, which is related to the distance between the transmitter and the receiver [115]. In such a case, the SRI can be obtained based on the distribution function of the $N_{\rm bin}$ energy samples (bins) at the energy detector output (see Fig. 8). In [51], a model for wideband ranging was proposed together with the PDF of each energy bin b_i , $f_{b_i}(b_i|\tau, \eta_{\rm h}, \eta_{\rm d})$, and the probability mass function (PMF) of the selected bin i, $f_{\rm i}(\hat{\imath}|\tau, \boldsymbol{\eta}_{\rm h}, \boldsymbol{\eta}_{\rm d})$ for a variety of ranging algorithms, where $\eta_{
m h}$ and $\eta_{
m d}$ are parameter vectors representing the wireless channel and the energy detector, respectively. Such a model is essential for obtaining the SRI from the energy detector output samples. The size of the observation set is important for computation and communication of the SRI; therefore, alternative methods based on reduced data sets of the observations were proposed in [225]. In particular, the SRI for a given observation of the energy bins b can be written as¹¹

$$\mathcal{L}_{\boldsymbol{b}}(\tau) = \prod_{i=0}^{N_{\text{bin}}-1} f_{\mathsf{b}_i}(b_i | \tau, \boldsymbol{\eta}_{\mathrm{h}}, \boldsymbol{\eta}_{\mathrm{d}}).$$
(51)

This is referred to as energy-based soft decision (ESD) [see Fig. 8(a)] and is obtained from a data set of size

¹¹The likelihood of the TOA is strictly related to that of the distance.

 $N_{\rm bin}$ (reduced by a factor $N_{\rm sb}$, the number of samples per bin, compared to SRI obtained from the complete set of received waveform samples). SRI can also be obtained from the PMF of the selected bin index as

$$\mathcal{L}_{\hat{i}}(\tau) = f_{i}(\hat{i}|\tau, \boldsymbol{\eta}_{h}, \boldsymbol{\eta}_{d}).$$
(52)

This is referred to as threshold-based soft decision (TSD) [see Fig. 8(a)] and is obtained from a data set of size one (reduced by a factor $N_{\rm sb} N_{\rm bin}$ compared to SRI obtained from the complete set of received waveform samples). The SRI provided by the likelihood functions (51) or (52) can be used for SI-based localization.¹²

B. Selection of Representative Measurements

Accurate LoT is challenging in harsh propagation conditions, where multipath, clutter, and signal obstructions can give erroneous measurements that are not representative of the positional states. These measurements, also called non-representative outliers [226], can adversely impact the localization performance [131]–[133]. In the context of LoT, it is particularly important to develop lowcomplexity techniques that select a measurement subset $\mathcal{Y}_{sel} \subseteq \mathcal{Y}$ containing the measurements that are more representative of positional states.

We now describe the measurement selection techniques that do not require the knowledge of the wireless environment and rely only on features extracted from the received waveform samples [130]. Consider a vector

$$\boldsymbol{\nu}_{ij} = \left[\nu_{ij}^{(0)}, \nu_{ij}^{(1)}, \dots, \nu_{ij}^{(N_{\rm d}-1)}\right]^{\rm T}$$

of N_d indicator samples for the pair (i, j). In the case of energy detection, $\nu_{ij}^{(q)}$ is related to the energy of the samples within the *q*th time interval (dwell time). Table 1 presents the temporal and amplitude features based on the vector $\boldsymbol{\nu}_{ij}$ for selecting the observations that are representative of the nodes positions (i.e., less affected by multipath, noise, and obstruction-loss). In particular, timebased selection features are inter-quartile range IQR_{ij} , variance $\tilde{\sigma}_{ij}^2$, kurtosis $\tilde{\kappa}_{ij}$, and skewness $\tilde{\chi}_{ij}$. Amplitudebased selection features are maximum value M_{ij} , sample variance s_{ij}^2 , sample range r_{ij} , and sample skewness c_{ij} . For each scenario, it is essential to choose the selection feature $h(\boldsymbol{\nu}_{ij}) \in \{IQR_{ij}, \tilde{\sigma}_{ij}^2, \tilde{\kappa}_{ij}, \tilde{\chi}_{ij}, M_{ij}, s_{ij}^2, r_{ij}, c_{ij}\}$ or a combination of them based on its relationship with the localization performance [130].

VII. CASE STUDIES

This section compares the performance of SVE-based, DP, and SI-based techniques in two case studies corresponding

¹²The SRI can also be used for SVE-based localization; in fact, the maximum of the SRI enables the determination of DEs for position inference in classical two-stage localization.

Table 1 Time- and Amplitude-Based Measurement Sele	ection Features
--	-----------------

Sample distributions/statistics	Time-based selection features	Amplitude-based selection features
$\tilde{f}_{ij}(q) = \nu_{ij}^{(q)} \Big(\sum_{q=0}^{N_{\rm d}-1} \nu_{ij}^{(q)} \Big)^{-1}$	$IQR_{ij} = \tilde{F}_{ij}^{-1}(0.75) - \tilde{F}_{ij}^{-1}(0.25)$	$M_{ij} = \max_q \nu_{ij}^{(q)}$
$\tilde{F}_{ij}(x) = \sum_{q \le x} \tilde{f}_{ij}(q)$	$\tilde{\sigma}_{ij}^2 = \tilde{\mu}_{ij}^{(2)}$	$s_{ij}^2 = \frac{1}{N_{\rm d} - 1} \sum_{q=0}^{N_{\rm d} - 1} \left[\nu_{ij}^{(q)} - \left(\frac{1}{N_{\rm d}} \sum_{q=0}^{N_{\rm d} - 1} \nu_{ij}^{(q)} \right) \right]^2$
$m_{ij} = \sum_{q=0}^{N_{\rm d}-1} q \tilde{f}_{ij}(q)$	$ ilde{\kappa}_{ij} = rac{ ilde{\mu}_{ij}^{(4)}}{(ilde{\mu}_{ij}^{(2)})^2}$	$r_{ij} = \max_{q} \nu_{ij}^{(q)} - \min_{q} \nu_{ij}^{(q)} $
$\tilde{\mu}_{ij}^{(n)} = \sum_{q=0}^{N_{\rm d}-1} (q - m_{ij})^n \tilde{f}_{ij}(q)$	$\tilde{\chi}_{ij} = \frac{\tilde{\mu}_{ij}^{(3)}}{(\tilde{\mu}_{ij}^{(2)})^{3/2}}$	$c_{ij} = \frac{1}{N_{\rm d} \left(s_{ij}^2\right)^{3/2}} \sum_{q=0}^{N_{\rm d}-1} \left[\nu_{ij}^{(q)} - \frac{1}{N_{\rm d}} \left(\sum_{q=0}^{N_{\rm d}-1} \nu_{ij}^{(q)}\right)\right]^3$

to the following scenarios:

1) noisy features and NLOS detection; and

2) IEEE 802.15.4 a standard.

In each scenario, measurements are obtained in different wireless environments.

Before delving into the performance comparison in each case study (CS), a discussion on the complexity of the SVE-based, DP, and SI-based techniques is given. The SVE-based technique does not require an off-line phase (training) and relies only on a single value per measurement. The DP technique requires prior knowledge of the channel model. If such a model is unknown, then DP uses an off-line phase to estimate the channel response (from multiple received waveforms for each anchor-agent distance).¹³ The SI-based technique requires an off-line phase to determine a generative model for the SFI (however, it does not require multiple received waveforms for each anchor-agent distance) [55]. In the on-line phase, DP technique computes a likelihood function that depends on the entire received waveform, resulting in high computational complexity, whereas the SI-based technique benefits from a dimensionality reduction step, resulting in significantly lower complexity despite the moderate information loss.

A. CS-I: Measurements Based on Noisy Features and NLOS Detection

Consider a network in a 100 m \times 100 m area with four anchors and a varying number of agents all randomly deployed therein. This CS compares the performance of SVE-based localization, DP, and SI-based localization in terms of root-mean-square error (RMSE) together with the position error bound (PEB) as a benchmark.¹⁴ The measurement set is composed of noisy features and NLOS detector output. The noisy features are related to ranges and/or angles according to (14) and (15), and the NLOS detector error follows (1). Specifically, we consider $\epsilon_{\text{NLOS}} = \epsilon_{\text{LOS}} = \epsilon$, $p_{\text{NLOS}} = 0.4$, and $\sigma_{\text{NLOS}} = \sigma_{\text{LOS}} = \sigma$ with $\sigma = 2$ meters for range measurements and $\sigma = 2$ degrees for angle measurements. We compare the SVE-based and SI-based techniques using the same measurements for inferring agent positions. In particular, SVE-based localization employs the Gaussian measurement model with mean and variance given, respectively, by (2) and (3). On the other hand, SI-based localization exploits SFI according to (13) and (16) for inferring agent positions based on the posterior distribution given by (19), (21), (23), or (25) for different levels of spatial and temporal cooperation.

Fig. 9 shows the localization performance based on range measurements as a function of the obstructed propagation bias β for different values of ϵ . Notice that SRI-based localization provides significant performance improvement and robustness to NLOS detection errors compared with DE-based localization. Also, observe that exploiting SRI enables the filling of most of the performance gap between DE-based localization and PEB. Similar observations can be made from Fig. 10, which shows the localization performance based on angle measurements for SAI- and AE-based localization.

Now, consider the fusion of range and angle measurements. Fig. 11 shows the localization performance as a function of the obstructed propagation bias β for different values of ϵ .¹⁵ Notice that SI-based localization exploiting both SRI and SAI provides significant performance improvement and robustness to NLOS detection errors compared to SVE-based localization using both DE and AE. Also, observe that the performance of SI-based localization approaches the PEB.

Consider spatial cooperation among agents. Fig. 12 shows the localization performance based on range measurements as a function of the number of cooperating agents for obstructed propagation bias $\beta = 20$ m and different values of ϵ . Notice that SRI-based localization provides significant performance improve-

¹³In the IEEE 802.15.4 a scenario, waveforms are processed in the time domain and a covariance matrix is obtained for each anchor–agent distance [141].

¹⁴PEB is the square root of the right-hand side of (29), which is independent of the specific localization technique used and serves as a benchmark for the MSE of unbiased position estimators.

¹⁵For example, $\beta = 20$ indicates that the bias on range measurements is of 20 m and the bias on angle measurements is of 20°.

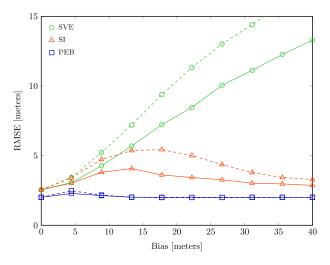


Fig. 9. Localization performance based on range measurements as a function of obstructed propagation bias for $\epsilon = 0.1$ (solid line) and 0.2 (dashed line). The performance of SVE-based localization (green circle) and SI-based localization (red triangle) as well as the PEB (blue square) are shown.

ment and robustness to NLOS detection errors compared to DE-based localization. Also, observe that exploiting SRI enables the filling of most of the performance gap between the DE-based localization and PEB. Note also that SRI-based localization exploits spatial cooperation better and approaches to the PEB faster with the number of cooperating agents compared to DE-based localization.

Now, consider navigation with temporal and spatiotemporal cooperation among agents. In such a scenario, each agent follows a circular trajectory (a radius of 20 m centered at a random position) at a speed of 0.625 m/s. The dynamic model for position inference is

$$\Phi_{\mu}(p^{(n)}, p^{(n-1)}) = \varphi(p^{(n)} - p^{(n-1)}; \mathbf{0}, \sigma_{d}^{2} \mathbf{I})$$

where $\sigma_{\rm d} = 0.6$ m and the localization update rate is $1/(t_n - t_{n-1}) = 1$ Hz for all *n*. First, consider temporal cooperation only. Fig. 13 shows the localization performance based on range measurements as a function of the time step for obstructed propagation bias β = 20 m and different values of ϵ . Notice that SRI-based navigation with temporal cooperation provides significant performance improvement and robustness to NLOS detection errors compared to DE-based navigation. Also, observe that exploiting SRI enables the filling of most of the performance gap between DE-based navigation and PEB. We now quantify the benefits due to spatial, in addition to temporal, cooperation. Fig. 14 shows the localization performance as a function of the time step and the number of cooperating agents in the same scenario considered in Fig. 13. Notice that SRI-based navigation exploits spatiotemporal cooperation better than DE-based localization by accentuating the performance improvement and

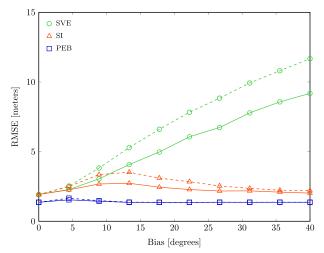


Fig. 10. Localization performance based on angle measurements as a function of obstructed propagation bias for $\epsilon = 0.1$ (solid line) and 0.2 (dashed line). The performance of SVE-based localization (green circle) and SI-based localization (red triangle) as well as the PEB (blue square) are shown.

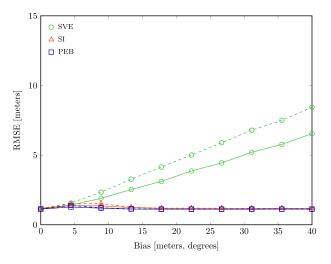


Fig. 11. Localization performance based on range and angle measurements as a function of obstructed propagation bias for $\epsilon = 0.1$ (solid line) and 0.2 (dashed line). The performance of SVE-based localization (green circle) and SI-based localization (red triangle) as well as the PEB (blue square) are shown.

robustness to NLOS conditions. Moreover, SRI-based localization with spatiotemporal cooperation approaches to the PEB faster with the number of cooperating agents compared to DE-based localization.

B. CS-II: Measurements Based on IEEE 802.15.4a Standard

Consider a network in a 20 m \times 20 m area with four anchors located at the corners of the square and agents randomly deployed therein. This CS compares the performance of SVE-based localization, DP, and SI-based localization in terms of localization error outage (LEO) defined as the empirical probability that the localization error is above a target value. The anchors emit

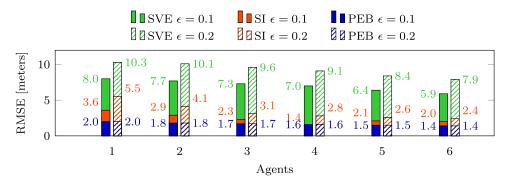


Fig. 12. Cooperative localization: localization accuracy and performance benchmark for different numbers of cooperating agents.

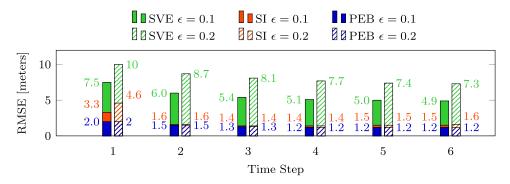


Fig. 13. Non-cooperative navigation: navigation accuracy and performance benchmark for different time steps.

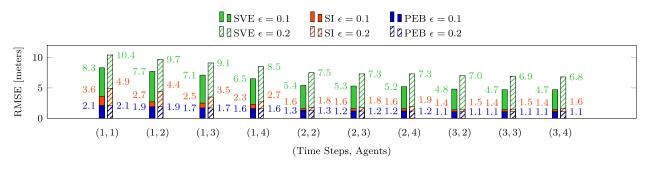


Fig. 14. Cooperative navigation: navigation accuracy and performance benchmark for different time steps and numbers of cooperating agents.

UWB root raised cosine pulses (roll-off factor of 0.6 and pulsewidth parameter of 0.95 ns) in the European lower band [3.1, 4.8] GHz with maximum power spectral density -42 dBm/MHz. The emitted pulses propagate through a multipath channel modeled according to the IEEE 802.15.4 a standard for indoor residential environments with probability $p_{\rm NLOS}$ of being in NLOS conditions. The signal-to-noise ratio at 1 m from the transmitter is 30 dB. SVE-based technique uses DE from each anchor, which is obtained from the delay $\tau_{\rm max}$ corresponding to the maximum correlation value between the received waveform and the transmitted pulse. The DP technique processes the received waveform according to the algorithm proposed in [141] with covariance matrices estimated from the received waveform samples during the off-line phase. The SI-based technique employs a three-modal Gaussian

generative model and exploits dimensionality reduction by considering $\psi(y)$ as a vector of four elements, including $\tau_{\rm max}$, the maximum value of the correlation, and two principal components obtained from PCA as in [55]. We compare SVE-, DP, and SI-based techniques for inferring agent positions based on the MMSE criterion using the same measurements.

Fig. 15 shows the LEO based on the received waveform measurements generated according to IEEE 802.15.4 a standard for the indoor residential and the outdoor channel models with $p_{\rm NLOS} = 0.2, 0.5, and 0.8$. Notice that SIbased localization exploiting SRI provides significant LEO improvement as well as robustness to NLOS propagation conditions compared to DP and SVE-based localization. For example, in indoor residential channel with $p_{\rm NLOS} =$ 0.2, the localization error is above 4 m in about 40% of

The proposed approach exploits SI that combines SFI

and SCI extracted from measurements and contextual

data, respectively. We described efficient techniques for

learning and exploiting the SI based on the reduced data

sets. Various case studies are presented for different wire-

less environments. In particular, the localization perfor-

mance is quantified for sensing measurements based on

noisy features and NLOS detection, and IEEE 802.15.4a

standard. The results show that SI-based localization sig-

nificantly outperforms DP and SVE-based localization,

especially in harsh propagation conditions. Indeed, SI-

based techniques are vital for LoT, especially when devices

are designed for communication rather than for localiza-

tion. Furthermore, the exploitation of SI offers robustness

to wireless propagation conditions, thereby opening the

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way to a new level of accuracy for the LoT.

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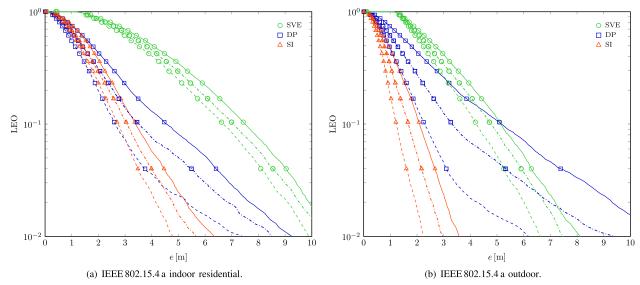


Fig. 15. LEO in two IEEE 802.15.4 a channels with different values of NLOS probability p_{NLOS} = 0.2 (dashed line), 0.5 (dotted-dashed line), and 0.8 (solid line). The performance of SVE-based localization (green circle), DP (blue square), and SI-based localization (red triangle) is shown.

cases for DE-based localization, 4% of cases for DP, and 2% of the cases for SI-based localization. In more severe NLOS propagation conditions with $p_{\rm NLOS} = 0.8$, the localization error is above 4 m in about 50% of cases for DE-based localization, 13% of cases for DP, and only 6% of the cases for the SI-based localization. In the outdoor channel with $p_{\rm NLOS} = 0.2$, the localization error is above 3 m in about 27% of cases for DE-based localization, 4% of cases for DP, and 2% of the cases for SI-based localization. With $p_{\rm NLOS} = 0.8$, the localization error is above 3 m in about 41% of cases for DE-based localization, 26% of cases for DP, and only 2% of the cases for the SI-based localization. This shows that also in IEEE 802.15.4 a standard scenario, SI-based localization is superior to DP and SVE-based localization, especially in harsh propagation conditions.

VIII. FINAL REMARK

This paper introduced the concept of LoT and proposed a new approach for accurate inference of positional states.

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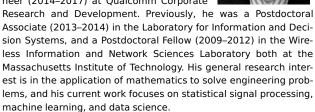
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